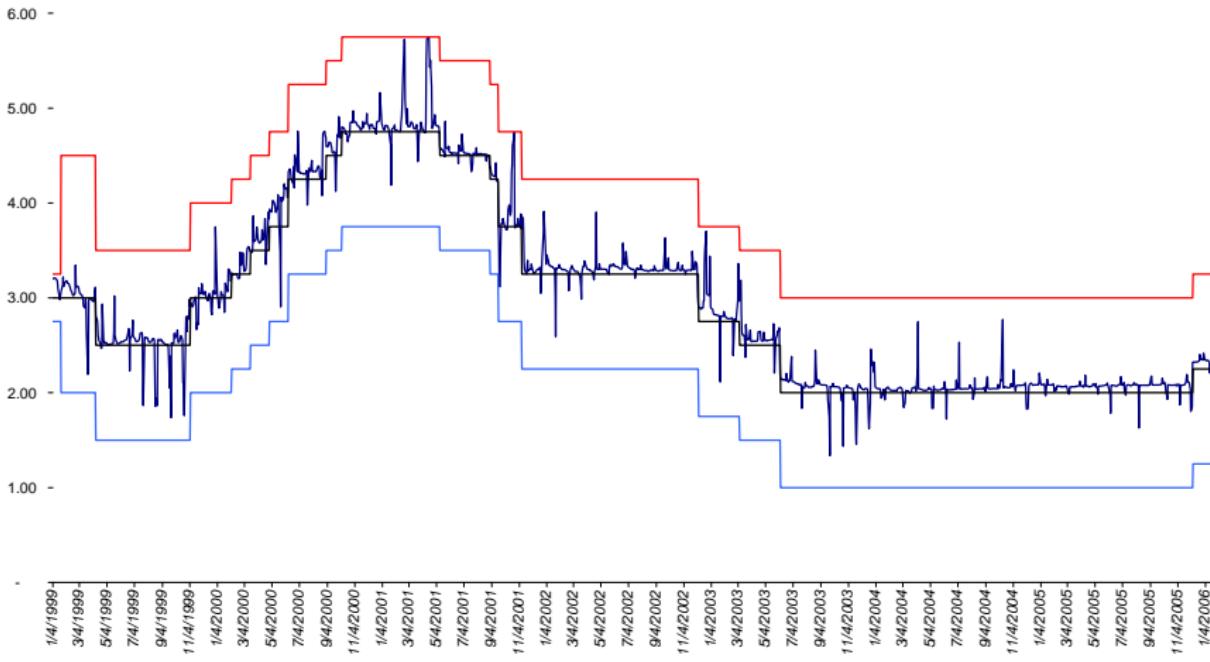


# **Monetary Policy in a Channel System**

Aleksander Berentsen  
University of Basel

Cyril Monnet  
Federal Reserve Bank of Philadelphia

**EONIA - Euro OverNight Index Average**  
Source: ECB

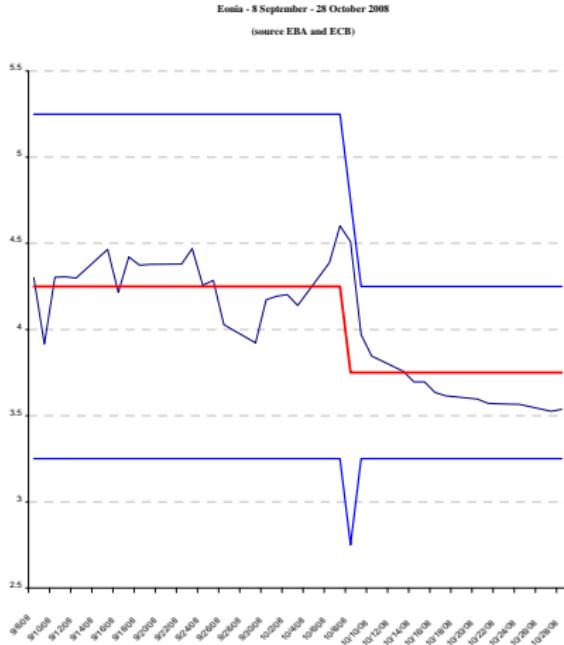
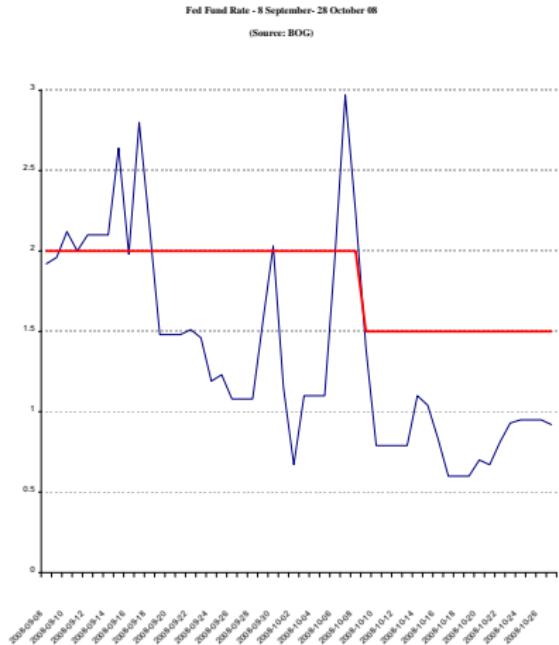


## Features of “pure” channel systems

- Standing facilities
- All CB loans are secured with collateral (typically REPOS)
- Few or no open market operations
- Money market allocates reserves; reserves management

## This Paper

- ... is on the optimal design of the MP implementation framework, given the CB uses a “pure” channel system.
- ...is not on the optimal monetary policy response to shocks.



# Objectives

- Optimal interest-rate corridor.
- Shift of corridor vs. changing the size.
- Implications of collateral requirements for the optimal policy.
- Steering money market rates without open market operations.

# Environment

- Based on current CB practice as much as possible.
- Version of Lagos and Wright (2005).
- Time discrete and infinite.
- $[0, 1]$  continuum of  $\infty$ -lived agents (banks/households).  
Anonymity.
- Walrasian markets open/close sequentially, in each  $t$ .

# Environment

**Settlement market:** Settle claims by trading a general good.  
Adjust money and collateral holdings.

**Money market:** Signals on liquidity needs. Borrow/lend  
money.

**Goods market (liquidity shock):**

- Produce with probability  $n$  at costs  $c(q_s) = q_s$
- Consume with probability  $1 - n$  and get  $u(q)$

**Standing facilities:**

Open before and after the goods market.

- Borrow from lending facility against collateral at rate  $i_\ell$ ,
- Deposit money at rate  $i_d$

# Collateral

- General goods can be ‘stored’ at the CB.
- Return in  $t + 1$  is  $R \geq 1$  with  $\beta R < 1$ .
- $1 + r = 1/\beta$  implies  $R < 1 + r$ .

## Benchmark: First Best Allocation

Expected lifetime utility of a representative agent

$$(1 - \beta)\mathcal{W} = (1 - n)[u(q) - q] + (\beta R - 1)b$$

First best allocation  $(q^*, b^*)$ , where:

$$u'(q^*) = 1, \text{ and } b^* = 0.$$

*Decentralization:*

Anonymity implies money is necessary.

# Money

- Central bank prints/burns paper money at not cost. Fiat.
- CB has no fiscal authority. No lump-sum transfers.
- Endogenous growth rate

$$M_t = M_{t-1} - (1 - n)i_\ell L_{t-1} + ni_d D_{t-1}.$$

- Stationary equilibrium

$$\phi M = \phi_{+1} M_{+1} \text{ and denote } \gamma = M_{+1}/M$$

## **No Money Market**

(signal totally uninformative)

# Symmetric Stationary Equilibrium

**Settlement stage:**

$$W(m_{-1}, b_{-1}, \ell, d) = \max_{h, m, b} -h + V(m, b)$$

$$\text{s.t. } \phi m + b = h + \phi m_{-1} + Rb_{-1} + \phi(1 + i_d)d - \phi(1 + i_\ell)\ell.$$

First-order conditions ( $m, b = \bar{m}, \bar{b}$  for all agents)

$$V_m \leq \phi \quad (= \text{ if } m > 0) \tag{1}$$

$$V_b \leq 1 \quad (= \text{ if } b > 0) \tag{2}$$

Envelope conditions

$$W_m = \phi; W_b = R; W_\ell = -\phi(1 + i_\ell); W_d = \phi(1 + i_d).$$

# Equilibrium

Goods market:

$$V(m, b) = (1 - n)V^b(m, b) + nV^s(m, b)$$

Sellers' problem

$$\begin{aligned} V^s(m, b) = \max_{q_s} \quad & \left\{ -q_s + \beta Rb + \beta \phi_+ (m + pq_s) (1 + i_d) \right\} \\ & + \beta [V(\bar{m}, \bar{b}) - \phi_+ \bar{m} - \bar{b}] \end{aligned}$$

FOC:  $p\beta\phi_+(1 + i_d) = 1$  (3)

# Equilibrium

## Buyers' problem

$$V^b(m, b) = \max_{q, \ell} \left\{ \begin{array}{l} u(q) + \beta Rb + \beta \phi_+ (m + \ell - pq) (1 + i_d) \\ \quad - \beta \phi_+ \ell (1 + i_\ell) \\ + \beta [V(\bar{m}, \bar{b}) - \phi_+ \bar{m} - \bar{b}] \end{array} \right\}$$

$$\text{s.t.} \quad pq \leq m + \ell \quad \text{and} \quad \phi_+ \ell (1 + i_\ell) \leq Rb$$

$$\text{FOC:} \quad u'(q) = \beta p \phi_+ (1 + i_\ell) + \lambda_\ell \quad (4)$$

# Equilibrium

Marginal value of money in the good market:

$$\phi \geq V_m = (1 - n)u'(q)/p + n(1 + i_d)\beta\phi_{+1} \quad (5)$$

$$\frac{\gamma/\beta - (1 + i_d)}{(1 + i_d)} \geq (1 - n) [u'(q) - 1] \quad (6)$$

Marginal value of collateral in the good market:

$$1 \geq V_b = (1 - n)\lambda_\ell\beta R / (1 + i_\ell) + \beta R \quad (7)$$

$$\frac{1/\beta - R}{R} \geq (1 - n) [u'(q)/\Delta - 1] \quad (8)$$

$$\Delta = (1 + i_\ell) / (1 + i_d).$$

# Equilibrium

## Definition

A symmetric stationary monetary equilibrium is a list  $(\gamma, q, z_\ell, z_m, b)$  satisfying (9)-(13) with  $z_\ell \geq 0$  and  $z_m \geq 0$ .

$$\frac{1/\beta - R}{R} \geq (1-n) [u'(q)/\Delta - 1] \quad (9)$$

$$\frac{\gamma/\beta - (1+i_d)}{(1+i_d)} \geq (1-n) [u'(q) - 1] \quad (10)$$

$$\gamma = 1 + i_d - (1-n)(i_\ell - i_d) \frac{z_\ell}{z_m}, \quad (11)$$

$$q = z_m + z_\ell \quad (12)$$

$$z_\ell = \beta R b / \Delta \quad (13)$$

# Equilibrium

## Proposition

For any  $\Delta \geq 1$  there exists a unique symmetric stationary equilibrium such that

- |                            |                       |                                |
|----------------------------|-----------------------|--------------------------------|
| $z_\ell > 0$ and $z_m = 0$ | <i>if and only if</i> | $\Delta = 1$                   |
| $z_\ell > 0$ and $z_m > 0$ | <i>if and only if</i> | $1 < \Delta < \tilde{\Delta}$  |
| $z_\ell = 0$ and $z_m > 0$ | <i>if and only if</i> | $\Delta \geq \tilde{\Delta}$ . |

where

$$\tilde{\Delta} = \frac{1 - n\beta}{1/R - n\beta} \text{ and } \Delta = \frac{1 + i_\ell}{1 + i_d}.$$

# Optimal Policy

Equilibrium with a positive amount of collateral  $1 \leq \Delta < \tilde{\Delta}$ .

This defines constraints on  $q$ :

- $\hat{q}$  is the level of consumption when  $\Delta = 1$ .
- $\tilde{q}$  is the level of consumption when  $\Delta > \tilde{\Delta}$

The central bank's problem is

$$\begin{aligned} \max_{q,b} \quad & (1 - n) [u(q) - q] + (\beta R - 1) b \\ \text{s.t. } & q = \beta b R F \left( \frac{R\beta(1-n)u'(q)}{1-nR\beta} \right) \\ & \hat{q} \geq q \geq \tilde{q} \end{aligned}$$

# Optimal Policy

## Proposition

*There exists a critical value  $\bar{R}$  such that if  $R < \bar{R}$ , then the optimal policy is  $\Delta \geq \tilde{\Delta}$ . Otherwise the optimal policy is  $\Delta \in (1, \tilde{\Delta})$ .*

- Since  $\beta R < 1$  it is **never** optimal to set a zero band.

$$\gamma = 1 + i_d - (1 - n)(i_\ell - i_d)\ell/m$$

- Set  $i_d = i_\ell$  (0 corridor) so that  $\gamma = 1 + i_d$ . Return on cash is  $\beta/\gamma$ .

Return on collateral is  $\beta R > \beta/\gamma$ , use only collateral, no money.

Collateral is socially inefficient.

- Rather, set  $i_\ell > i_d$ : Makes borrowing less attractive, reduce inflation, holding money more attractive.

## **Money Market**

(signal contains some information)

# Record Keeping

- Berentsen, Camera and Waller (2006).
- Operated by the CB. Identifies participants and verifies collateral.
- Cannot keep record of goods market transactions.

# Trade on the Money Market

**Two Types:**  $H$  (likely to be seller) and  $L$  (likely to be buyer)

- H-types lend money/L-types borrow money
- $\sigma^k$ : probability of  $k$ -type.
- $n^k$ : probability that a  $k$ -type turns seller.

## Agents' Problems

essentially the same as before, except

- Short selling constraints on the money market:

$$\phi_+ y^k (1 + i_m) \leq Rb \text{ and } m + y^k \geq 0.$$

- Borrowing constraint in the goods market:

$$\ell^k \leq \bar{\ell}^k \equiv \frac{Rb}{\phi_+ (1 + i_\ell)} - y^k \frac{(1 + i_m)}{(1 + i_\ell)}$$

# Equilibrium

Stationary equilibrium is determined by

$$\hat{\Delta} = \frac{1 + i_\ell}{1 + i_m} \quad \text{and} \quad \Delta = \frac{1 + i_\ell}{1 + i_d}$$

# Equilibrium

Short-selling constraints are nonbinding, then

$$\hat{\Delta} = \frac{\Delta}{n\beta R(1 - \Delta) + \Delta} \quad (14)$$

$$u'(q^k) = \frac{n^k}{1 - n^k} \Delta \frac{1 - n\beta R}{n\beta R}, \quad k = H, L. \quad (15)$$

## Definition

A symmetric stationary equilibrium where no short-selling constraint is binding in the money market is a time-invariant list  $(\hat{\Delta}, q^L, q^H)$  satisfying (14) - (15) with  $b \geq 0$ ,  $z^L < \beta R b \hat{\Delta} / \Delta$  and  $z^H > -z_m$ .

# Equilibrium

Let  $n^H - n^L = \varepsilon$ . So that  $n^H = n + \sigma^L \varepsilon$  and  $n^L = n - \sigma^H \varepsilon$ .

## Proposition

*For any  $1 < \Delta < \tilde{\Delta}$  there exists a critical value  $\varepsilon_1 > 0$  such that if  $\varepsilon < \varepsilon_1$  a symmetric monetary equilibrium exists where no short-selling constraint in the money market binds.*

# Results

## 1) Money market rate and the corridor

$$\hat{\Delta} = \frac{\Delta}{n\beta R(1 - \Delta) + \Delta}$$

$$i_m = i_\ell - n\beta R(i_\ell - i_d)$$

- If  $n = 1/2$  and  $\beta R \rightarrow 1$ , then  $i_m \rightarrow (i_\ell + i_d)/2$ .
- If  $n = 1/2$  and  $\beta R < 1$ , then  $i_m > (i_\ell + i_d)/2$

## 2) Collateral requirement

$$u'(q^k) = \frac{n^k}{1 - n^k} \Delta \frac{1 - n\beta R}{n\beta R}$$

- Collateral modifies the real allocation.

# Results

## 3) Need to specify a corridor rule

- Symmetric increase of the corridor width leaves  $i_m$  constant but *has* real effects:

$$u'(q^k) = \frac{n^k}{1 - n^k} \Delta \frac{1 - n\beta R}{n\beta R}$$

- Need to specify a corridor rule as well as an interest rate rule.

## Summary and final remarks

- Details of implementation framework matter.
- The more costly the collateral, the larger the band optimally. The least costly the collateral,  $i_m \rightarrow (i_\ell + i_d)/2$ .
- Shifting the corridor  $\delta = i_\ell - i_d$  up increases the money market rate  $i_m$ .
- It does not matter whether the deposit rate is set to zero (i.e. deposits are not allowed).

**EONIA - Euro OverNight Index Average  
and Eurepo - reference rate for the Euro GC repo market**  
*Source: European Banking Federation and ECB*

