

The Effect of Maternal Labor Supply on Children: Evidence from Bunching

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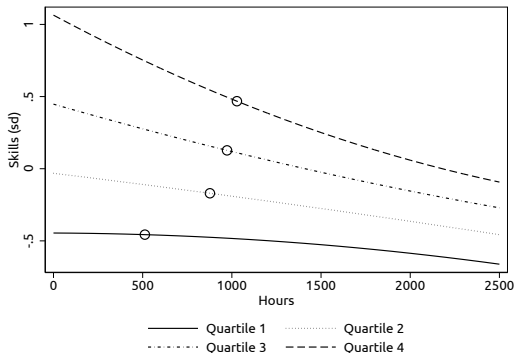
Motivation

- ▶ Maternal labor supply has increased in recent decades (Eckstein and Lifschitz 2011, Fogli and Veldkamp 2011).
- ▶ Quality parent-child interactions known to be important for child development (e.g. Todd and Wolpin 2007).
- ▶ How might maternal labor supply affect children in the short-run?
 1. time channel: **more** time at work \implies **less** time at home
 2. income channel: **more** time at work \implies **more** income
- ▶ Many policies (family leave, paid childcare, child tax credits, other tax changes, etc.) might affect maternal labor supply.

This Paper

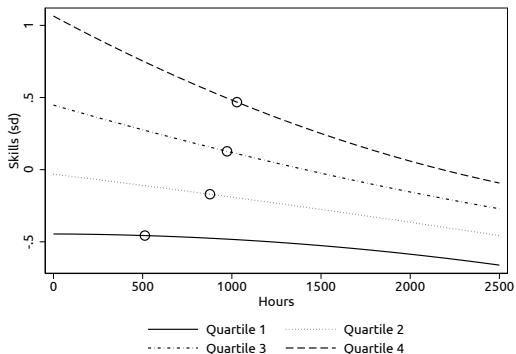
- ▶ We estimate the effect of maternal work hours during first 3 years of life on children's skills around age 6.
- ▶ We use a new approach leveraging bunching at zero to deal with endogeneity (Caetano, Caetano and Nielsen 2021).
- ▶ We focus on heterogeneous effects:
 - ▶ by the skill of the mother
 - ▶ by the quantity of her labor supply
- ▶ Why mothers and not all parents?
 - ▶ data limitations, prior literature
 - ▶ greater variation in maternal labor supply

Preview of Results: by Quartile of Maternal AFQT



- ▶ Negative effects on children's cognitive skills in the short-run.
- ▶ Less negative for less skilled mothers, except those who work long hours.

Preview of Results: by Quartile of Maternal AFQT



- ▶ Why is higher skilled maternal labor supply so detrimental for children's skills in the short-run?
 - ▶ Last hour is more costly for those working longer hours.
 - ▶ Money insufficient in the short-run to compensate for high-skill mother-child interactions.

Additional Heterogeneity: by Pre-Birth Maternal Wage

- ▶ Think of two similarly skilled mothers with different earnings (e.g. through college major or occupation).
- ▶ Try to vary income holding quality of home interaction constant. The skills that separate them are well-valued in the job market, but not necessarily in interactions with a young child.
- ▶ Money helps, but is not enough: Even highly-skilled, highly-paid mothers cannot fully compensate for their absence with money.
- ▶ Flexible schedules and work-from-home may be a better policies than giving financial incentives to work.

Literature

- ▶ NLSY79/CNLSY. Effect of **working hours while child is 0-3** on **child's early outcomes**.
 - ▶ Negative effects:
Ruhm 2004, Bernal 2008, Desai et al. 1989, Baydar and Brooks-Gunn 1991, Hill and O'Neill 1994, Baum 2003
 - ▶ Zero effects:
James-Burdumy 2005, Parcel and Menaghan 1994, Blau et al. 1992, Waldfogel et al. 2002
 - ▶ Positive effects:
Vandell and Ramanan 1992 (low-income families)
- ▶ More recent literature: focus on time-money trade-off
 - ▶ Negative time effects not fully offset by income effects:
Agostinelli and Sorrenti (2021): NLSY79/CNLSY. **Effect of working hours while child is 4-16** on **contemporaneous child outcome**.
 - ▶ Income effects fully offset negative time effects:
Nicoletti, Salvanes and Tominey (2022): Norwegian data. Effect of **working hours while child is 0-5** on **outcome when child is 11-15**.

Data

NLSY79 (Mothers)

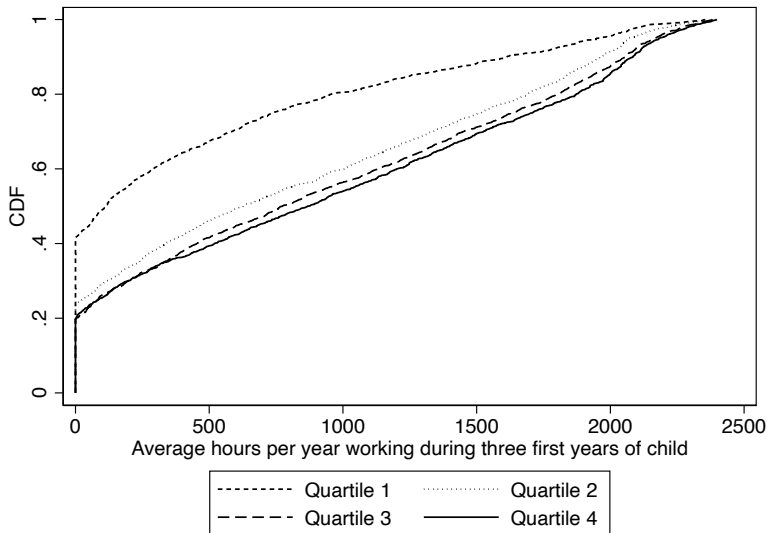
- ▶ AFQT, education, marital status, age at birth, hh income
- ▶ average hours worked over three years following birth
- ▶ exclude three months immediately after birth (maternity leave)
- ▶ family structure

CNLSY (Children)

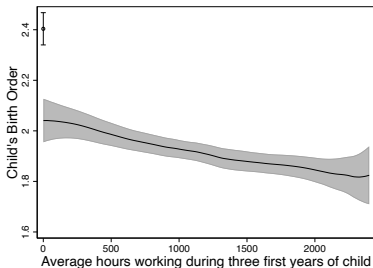
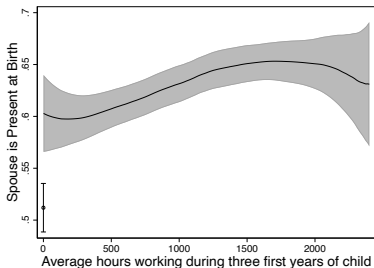
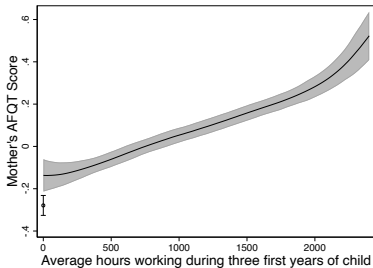
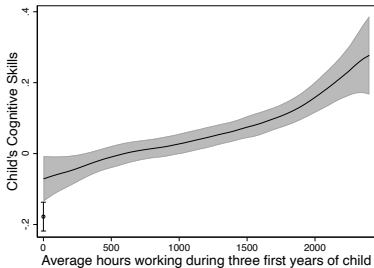
- ▶ race/ethnicity, sex
- ▶ cognitive skills – iterated principal factor analysis applied to PIAT math and reading scores, administered around age 6

Final sample consists of 6,924 mother-child pairs.

Bunching of Labor Supply



Selective Bunching



Intuition (No Controls)

Given skills S , labor supply L , and *desired* labor supply L^* ,

$$S = \alpha + \beta L + \delta L^* + \epsilon.$$

$L^* = L$ when $L^* \geq 0$. At $L = 0$, L^* indexes possibly confounding unobservables.

What is the effect of increasing hours from $L = l_0$ to $L = l_1$?

$$\underbrace{\mathbb{E}[S|L = l_1, L^* = l_1] - \mathbb{E}[S|L = l_0, L^* = l_0]}_{\text{what we observe}} =$$
$$\underbrace{\mathbb{E}[S|L = l_1, L^* = l_1] - \mathbb{E}[S|L = l_0, L^* = l_1]}_{\text{marginal treatment effect}} +$$
$$\underbrace{\mathbb{E}[S|L = l_0, L^* = l_1] - \mathbb{E}[S|L = l_0, L^* = l_0]}_{\text{selection bias}}$$

Intuition (No Controls) ▶ RDD

Usual approach turns off selection term. We turn off treatment effect term. At $L = 0$:

- ▶ treatment does not vary
- ▶ remaining variation in S informative about effect of unobservables (indexed by L^*) on skills
- ▶ if this “selection” effect can be identified, so can the treatment effect of interest

Like an “upside-down” RDD:

- ▶ “running variable” L varies continuously with L (trivially)
- ▶ unobservables L^* discontinuous at $L = 0$
- ▶ outcome discontinuities at $L = 0$ due to L^*
- ▶ dist. assumptions provide “first stage” of upside-down RDD

A Model of Constrained Choice

$$S = \beta L + g(X) + \epsilon, \quad \mathbb{E}[\epsilon | L, X] \neq 0$$

A Model of Constrained Choice

$$S = \beta L + g(X) + \overbrace{\delta \eta}^{\epsilon} + \varepsilon, \quad \mathbb{E}[\varepsilon | L, X, \eta] = 0$$

A Model of Constrained Choice

$$S = \beta L + g(X) + \overbrace{\delta \eta}^{\epsilon} + \varepsilon, \quad \mathbb{E}[\varepsilon | L, X, \eta] = 0$$

$$L^* = h(X) + \eta$$

$$L = \max\{0, L^*\}$$

A Model of Constrained Choice

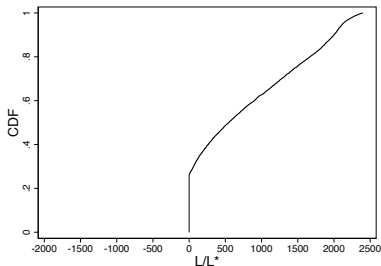
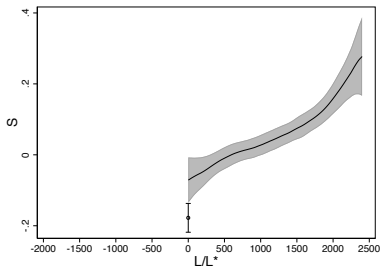
$$S = \beta L + g(X) + \overbrace{\delta \eta}^{\epsilon} + \varepsilon, \quad \mathbb{E}[\varepsilon | L, X, \eta] = 0$$

$$L^* = h(X) + \eta$$

$$L = \max\{0, L^*\}$$

$$\mathbb{E}[S | L, X] = \beta L + \underbrace{g(X) - \delta h(X)}_{m(X)} + \delta \underbrace{[L + \mathbb{E}[L^* | L = 0, X] 1(L = 0)]}_{\text{new regressor}}$$

Identification with Distributional Assumptions

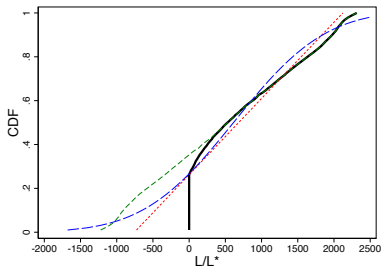
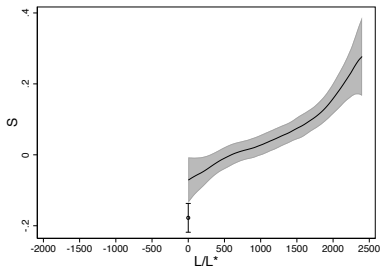


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Identification with Distributional Assumptions

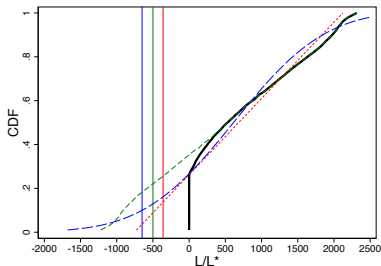
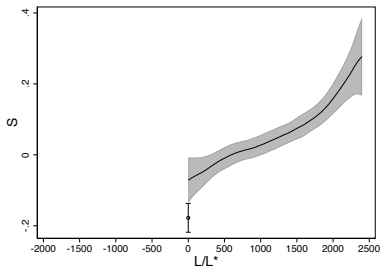


$$S = \beta L + g(X) + \delta \eta + \varepsilon, \quad \mathbb{E}[\varepsilon | L, X, \eta] = 0$$

$$L^* = h(X) + \eta, \quad \eta \sim \text{Normal, Uniform, or Symmetric}$$

$$\mathbb{E}[S | L, X] = \beta L + m(X) + \delta \underbrace{[L + \mathbb{E}[L^* | L = 0, X] 1(L = 0)]}_{\text{new regressor}}$$

Identification with Distributional Assumptions



$$S = \beta L + g(X) + \delta \eta + \varepsilon, \quad \mathbb{E}[\varepsilon | L, X, \eta] = 0$$

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$$\mathbb{E}[S | L, X] = \beta L + m(X) + \delta \underbrace{[L + \mathbb{E}[L^* | L = 0, X] 1(L = 0)]}_{\text{new regressor}}$$

$$S = \beta L + g(X) + \delta\eta + \varepsilon$$

	(i) No Controls	(ii) Controls	(iii) Het. Tobit	(iv) Het. Uniform	(v) Het. Symmetric
β	0.014** (0.001)	0.000 (0.001)	-0.016** (0.005)	-0.019** (0.006)	-0.019** (0.005)
δ			0.014** (0.004)	0.017** (0.005)	0.017** (0.005)

▶ empirical details

- ▶ +10 hrs/wk (over 3 years) lowers cog skills by 0.1 s.d.
- ▶ Context – 0.1 sd similar to
 - ▶ effect of a 1 sd improvement in teacher quality
 - ▶ effect of a 35% class size reduction
 - ▶ maternal labor effects in prior literature
- ▶ Non-cognitive effects directionally similar but not significant

Robustness

Identifying assumptions are (partially) testable.

- ▶ $\mathbb{E}[\epsilon|L, X] = 0$ ▶ linearity
- ▶ $\mathbb{E}[\epsilon|L, X, \eta] = 0$ ▶ truncation
- ▶ KS tests almost never reject full symmetry

We also assess the robustness/plausibility of our estimates.

- ▶ alternative samples ▶ diff. samples
- ▶ plausible degree of selection ▶ Oster (2019)
- ▶ violations in the distributional assumption ▶ dist. robustness
- ▶ alternative ways of controlling for observables ▶ clusters
- ▶ more flexible models for δ . ▶ $\delta(X)$

Heterogeneity by Maternal Skill and Hours

$$S = f(L, X; \theta) + g(X) + \delta(X)\eta + \varepsilon$$

A = AFQT score of the mother

$$\begin{aligned} f(L, X; \theta) &= (\beta + \beta_A A + \beta_L L + \beta_{AL} AL)L \\ \delta(X) &= \delta + \delta_A A \end{aligned}$$

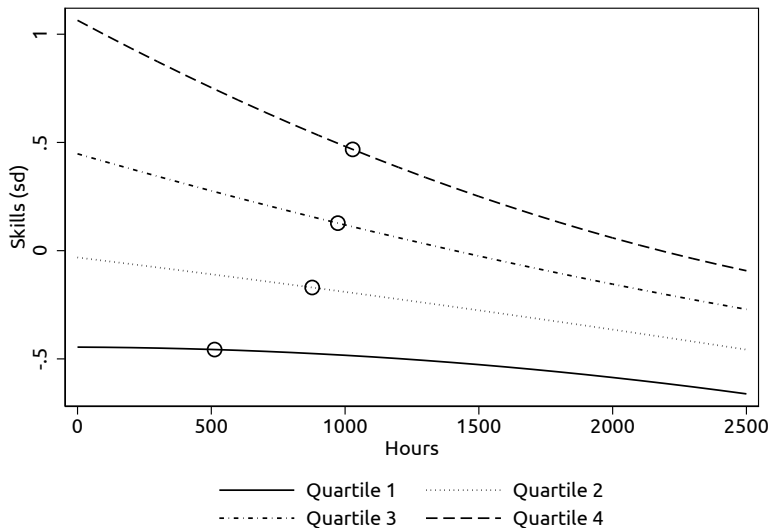
- ▶ $(\beta, \beta_A, \beta_L, \beta_{AL}, \delta, \delta_A)$ are identified (Caetano et al. 2021)
- ▶ higher order terms identified but not significant

Heterogeneity by Maternal Skill and Hours

	(i) No Controls	(ii) Controls	(iii) Het. Tobit	(iv) Het. Uniform	(v) Het. Symmetric
β	0.018** (0.004)	0.003 (0.003)	-0.023** (0.008)	-0.026** (0.010)	-0.030** (0.009)
β_A	0.047** (0.003)	-0.010** (0.004)	-0.017** (0.008)	-0.021** (0.009)	-0.026** (0.009)
$\beta_L (\times 1000)$	-0.004** (0.002)	-0.001 (0.001)	0.002 (0.002)	0.001 (0.002)	0.002 (0.002)
$\beta_{AL} (\times 1000)$	-0.015** (0.001)	0.003** (0.002)	0.004** (0.002)	0.004** (0.002)	0.004** (0.002)
δ			0.016** (0.005)	0.022** (0.007)	0.023** (0.006)
δ_A			0.005 (0.005)	0.009 (0.006)	0.013** (0.006)

- ▶ $\hat{\beta}_A < 0$ skill-intensity of skill production
- ▶ $\hat{\beta}_L > 0, \hat{\beta}_{AL} > 0$ positive income effects
- ▶ $\hat{\delta}_A > 0$ more positive selection for more skilled mothers

Visualizing the Heterogeneous Effects



Further Heterogeneity: by Pre-Birth Wage

$$S = f(L, X; \theta) + g(X) + \delta(X)\eta + \varepsilon$$

A = AFQT score, W = Pre-birth wage

$$f(L, X; \theta) = (\beta + \beta_A A + \beta_W W + \beta_L L + \beta_{AL} AL + \beta_{WL} WL)L$$

$$\delta(X) = \delta + \delta_A A + \delta_W W$$

- ▶ $(\beta, \beta_A, \beta_W, \beta_L, \beta_{AL}, \beta_{WL}, \delta, \delta_A, \delta_W)$ are identified
- ▶ For two mothers with the same skills, is the effect less negative for the higher-wage mother?

Heterogeneity by Maternal Skill, Wages, and Hours

	(i) No Controls	(ii) Controls	(iii) Het. Tobit	(iv) Het. Uniform	(v) Het. Symmetric
β	-0.004 (0.005)	-0.002 (0.004)	-0.009 (0.014)	-0.013 (0.026)	-0.017 (0.017)
β_A	0.039** (0.004)	-0.016** (0.004)	-0.027** (0.014)	-0.047** (0.023)	-0.035** (0.017)
β_W	0.007* (0.004)	0.001 (0.005)	0.014 (0.016)	0.029 (0.026)	0.018 (0.019)
$\beta_L (\times 1000)$	0.002 (0.002)	0.001 (0.002)	0.001 (0.002)	0.001 (0.002)	0.001 (0.002)
$\beta_{AL} (\times 1000)$	-0.012** (0.002)	0.005** (0.002)	0.006** (0.002)	0.007** (0.002)	0.007** (0.002)
$\beta_{WL} (\times 1000)$	-0.002 (0.002)	0.001 (0.002)	-0.000 (0.002)	-0.001 (0.002)	-0.000 (0.002)
δ			0.006 (0.010)	0.010 (0.022)	0.013 (0.013)
δ_A			0.008 (0.009)	0.027 (0.020)	0.015 (0.013)
δ_W			-0.009 (0.010)	-0.024 (0.021)	-0.014 (0.014)

Conclusion – Results

- ▶ Effect of maternal hours worked in a child's first 3 years on cognitive skills around age 6: **negative on average, very negative for high-skilled mothers.**
 - ▶ Last hour of work is more costly the longer the mother works?
No – effects are close to linear and slightly convex for high-skilled mothers.
 - ▶ Incremental earnings insufficient to offset direct time effect?
Yes, even for high-skilled, high-wage mothers. Estimates are noisy, though.
- ▶ Control for endogeneity using novel approach leveraging bunching of mothers at zero labor supply.
 - ▶ does not require instruments or special data structures
 - ▶ complementary to other identification methods
 - ▶ broadly applicable in empirical settings

Conclusion – Discussion

- ▶ What work-promoting policies would avoid negative effects on children's skills?
 - ▶ For low-skilled mothers: no negative effects unless mother works close to full time.
 - ▶ Increasing the financial rewards to working would likely be ineffective for higher-skilled mothers.
 - ▶ Flexible work arrangements may be particularly helpful for higher-skilled mothers.
 - maintain working hours and income while increasing time spent with children
 - ▶ Flexible work for partners may be complementary.

Introduction
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Data
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Identification Strategy
○○○○

Results
○○○○○○○

Conclusion
○○●

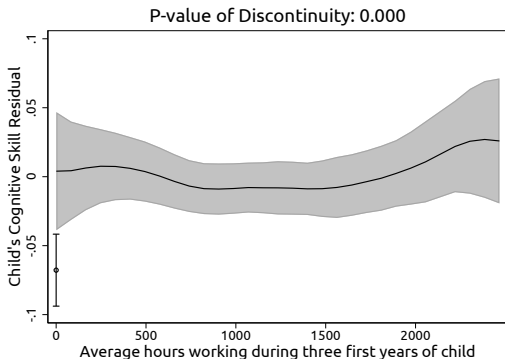
Appendix
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Thank you!

Estimation Details [▶ Back](#)

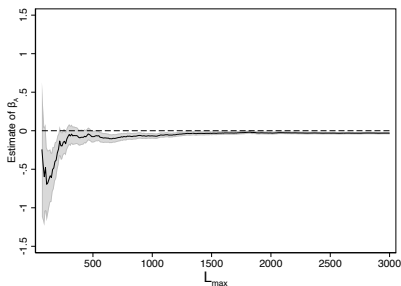
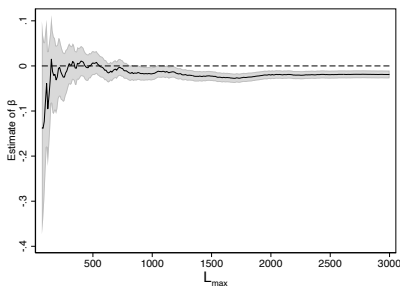
- ▶ It is a good idea to discretize X first, then use cluster indicators to approximate $m(X)$, $\delta(X)$ and $\mathbb{E}[L^* | L^* \leq 0, X]$.
- ▶ We use hierarchical cluster with 50 clusters in all reported results.
- ▶ Intuition: as the number of clusters increase, these approximations improve.
- ▶ See Caetano, Caetano and Nielsen (2021) for details.

Testing Assumption $\mathbb{E}[\epsilon|L, X] = 0$ [▶ Back](#)



$$S = \beta L + X' \tau + \sum_{k=1}^K \alpha_k \mathbf{1}(X \in \hat{C}_k) + \delta [L + \hat{\mathbb{E}}[L^* | L = 0, \hat{C}_K] \mathbf{1}(L = 0)]$$

Testing Assumption $\mathbb{E}[\varepsilon|L, X, \eta] = 0$

[▶ Back](#)

Restrict the sample to $L \leq L_{\max}$ for different values of L_{\max} .

Alternative Samples/Models

[▶ Back](#)

		(i) Uncorrected No Controls	(ii) Uncorrected Controls	(iii) Het. Tobit	(iv) Het. Uniform	(v) Het. Symmetric
Not Single	β	0.014** (0.001)	0.000 (0.001)	-0.016** (0.005)	-0.019** (0.006)	-0.019** (0.005)
	δ			0.014** (0.004)	0.017** (0.005)	0.017** (0.005)
Not College	β	0.012** (0.001)	0.001 (0.001)	-0.015** (0.005)	-0.019** (0.006)	-0.018** (0.006)
	δ			0.014** (0.004)	0.018** (0.005)	0.017** (0.005)
Other Income	β	0.013** (0.001)	-0.000 (0.001)	-0.016** (0.006)	-0.020** (0.007)	-0.019** (0.007)
	δ			0.013** (0.005)	0.017** (0.006)	0.017** (0.006)
$\delta(X)$ by Cluster	β	0.014** (0.001)	0.000 (0.001)	-0.014** (0.005)	-0.019** (0.007)	-0.017** (0.006)

Independent Evidence of Selection: Oster (2019) ▶ Back

Consider a regression of S on L , X , and *all confounders*, W .

- ▶ R_{max} is the R^2 of this hypothetical regression

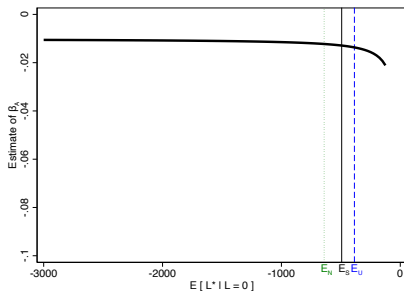
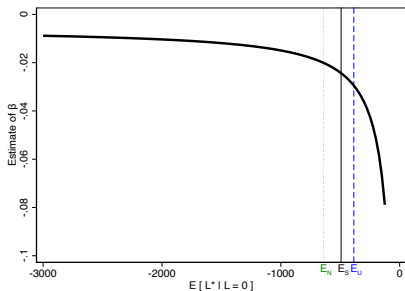
Fix the true value of β :

- ▶ let $\hat{\beta}$ be the OLS estimate of L in the uncorrected regression
- ▶ What value of $\delta_{Oster} = \left(\frac{\sigma_{L,W}}{\sigma_W^2} \right) / \left(\frac{\sigma_{L,X}}{\sigma_X^2} \right)$ has $\text{plim } \hat{\beta} = 0.000$?

	True $\beta = -0.019$					
R_{max}	0.50	0.60	0.70	0.80	0.90	1.00
δ_{Oster}	1.12	0.82	0.65	0.54	0.46	0.40

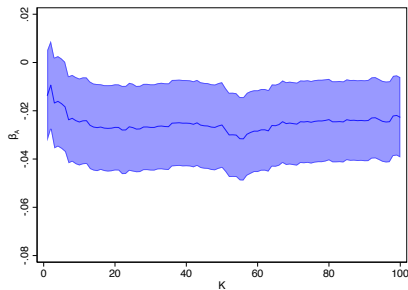
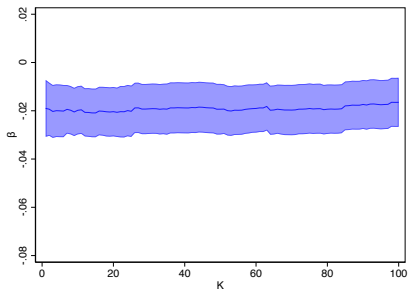
Observing an uncorrected estimate equal to what we find typically requires less selection on unobservables than observables.

Robustness to violations in distributional assumptions [▶ Back](#)



Black line shows β and β_A estimates for a wide range of assumed values of $\mathbb{E}[L^*|L=0, X]$.

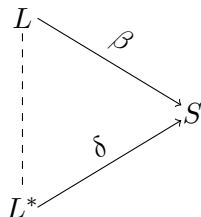
Changing the number of clusters

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Relation to RDD

[▶ Back](#)

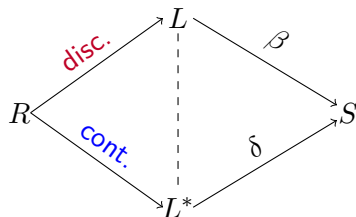
$$S = \alpha + \beta L + \delta L^* + \epsilon$$



Relation to RDD

[▶ Back](#)

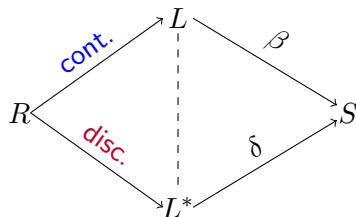
$$S = \alpha + \beta L + \delta L^* + \epsilon$$



Relation to RDD

[▶ Back](#)

$$S = \alpha + \beta L + \delta L^* + \epsilon$$

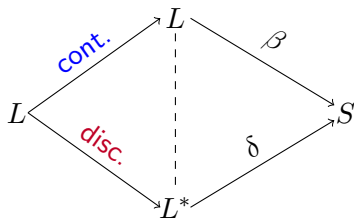


Relation to RDD

[▶ Back](#)

$$S = \alpha + \beta L + \delta L^* + \epsilon$$

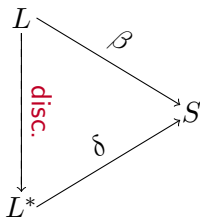
$$L = \max\{0, L^*\}$$



Relation to RDD [▶ Back](#)

$$S = \alpha + \beta L + \delta L^* + \epsilon$$

$$L = \max\{0, L^*\}$$



Cont. Treatment: $\lim_{l \rightarrow 0^+} \mathbb{E}[\beta L | L = l] - \mathbb{E}[\beta L | L = 0] = 0$

Disc. Endogeneity:

$$\lim_{l \rightarrow 0^+} \mathbb{E}[\delta L^* | L = l] - \mathbb{E}[\delta L^* | L = 0] = -\delta \mathbb{E}[L^* | L = 0]$$