

DISCUSSION OF:  
MONETARY POLICY IN A CHANNEL SYSTEM

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## THIS DISCUSSION

- (A) Key Features of the Model
- (B) Main Findings and Intuition
- (C) Discuss Robustness of the Policy Implications
  - ◇ Relax Assumption
  - ◇ Active Money Market

## (B) MAIN FINDINGS AND INTUITION

**Assumption ① - ④ imply First Best cannot be achieved:**

$$\text{Welfare} = (1 - n) \underbrace{[u(q) - q]}_{\text{trade surplus}} - \underbrace{(1 - \beta R)b}_{\text{collateral cost}}$$

$\Rightarrow$  First Best:  $b = 0$  and  $q = q^*$  with  $u'(q^*) = 1$

When  $b = 0$ , equilibrium money demand:

$$\underbrace{\frac{\gamma}{\beta(1 + i_d)}}_{\text{MC}} - 1 = \underbrace{(1 - n)(u'(q) - 1)}_{\text{MB}}$$

◇ Without ② or ④:  $\gamma = \beta$  and  $i_d = 0 \Rightarrow q = q^*$ .

◇ With ② and ④:  $\gamma \geq 1 + i_d > \beta \Rightarrow q < q^*$ .

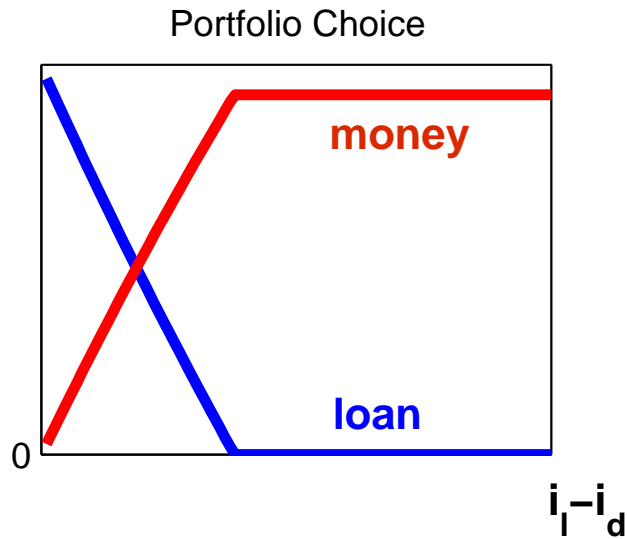
## (B) MAIN FINDINGS

Benchmark Case: When money market is inactive ( $\varepsilon = 0$ ):

Optimal Policy:

- Positive Interest Corridor  $i_l - i_d > 0$
- Zero Lump Sum Transfers  $\tau = 0$

(1) What's the equilibrium effect of interest corridors?

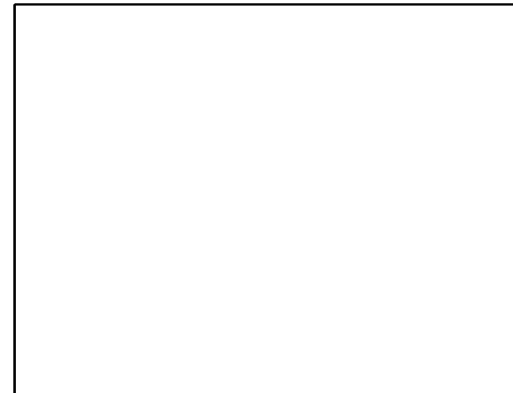


Proposition 1

$i_l \uparrow$  relative to  $i_d$

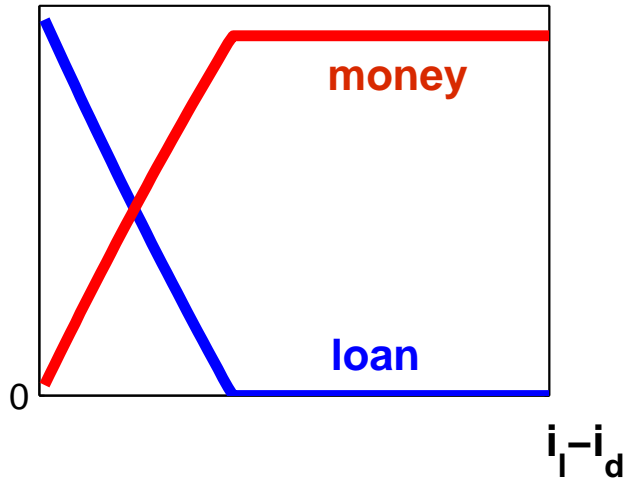
$\Rightarrow$  borrowing  $\downarrow$

$\Rightarrow$  money  $\uparrow$

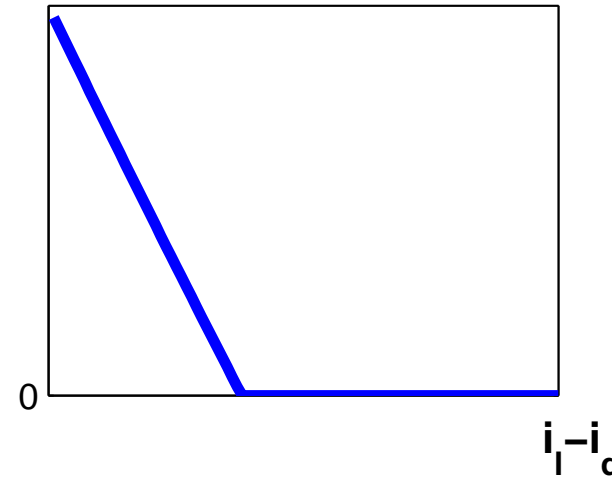


(1) What's the equilibrium effect of interest corridors?

Portfolio Choice



Collateral (b)



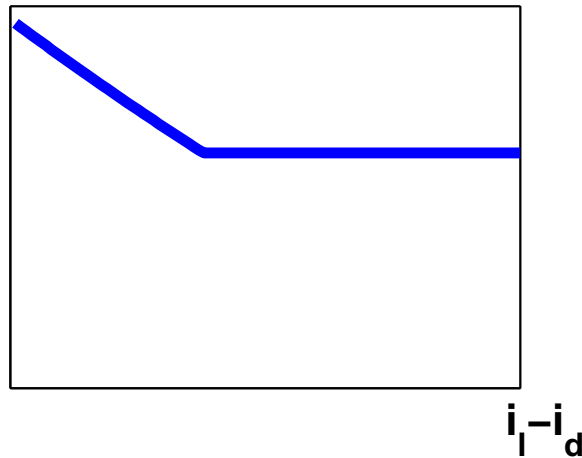
$i_l \uparrow$  relative to  $i_d$

borrowing ↓

⇒ collateral ↓

⇒ Welfare ↑

Consumption (q)



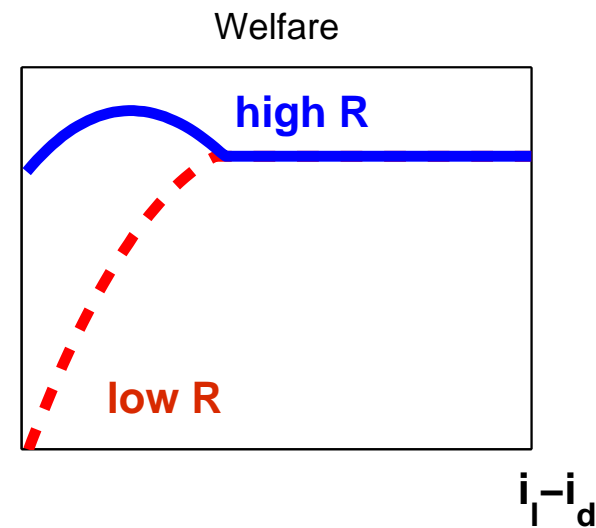
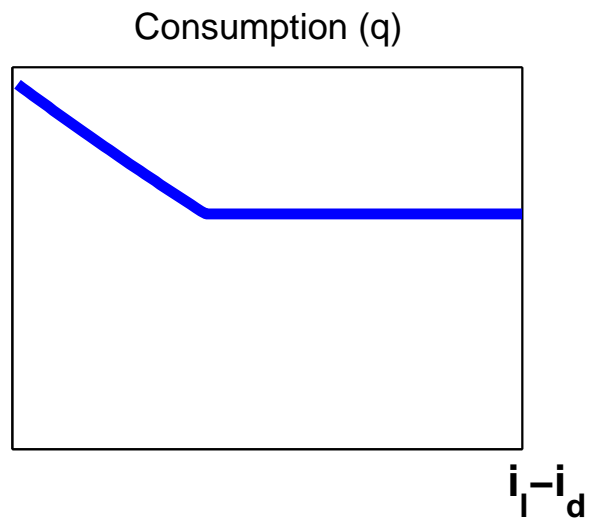
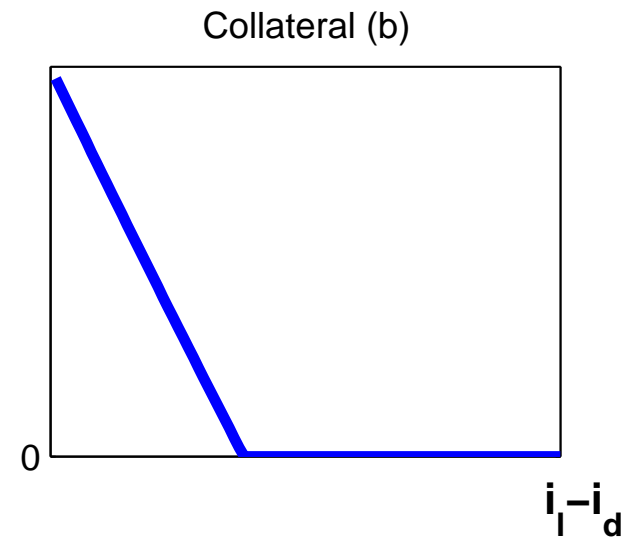
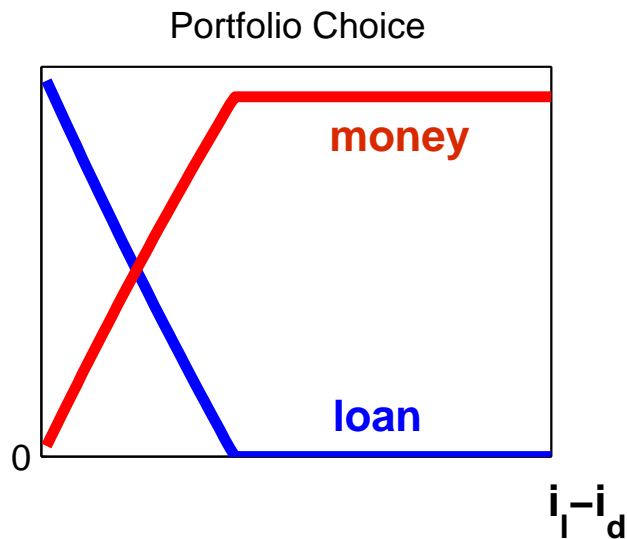
$i_l \uparrow$  relative to  $i_d$

borrowing ↓

⇒ consumption ↓

⇒ Welfare ↓

## (2) What is the optimal policy?



### Proposition 2

Optimal Policy:

$b$  is costly (low  $R$ )

$\Rightarrow$  high  $i_l$

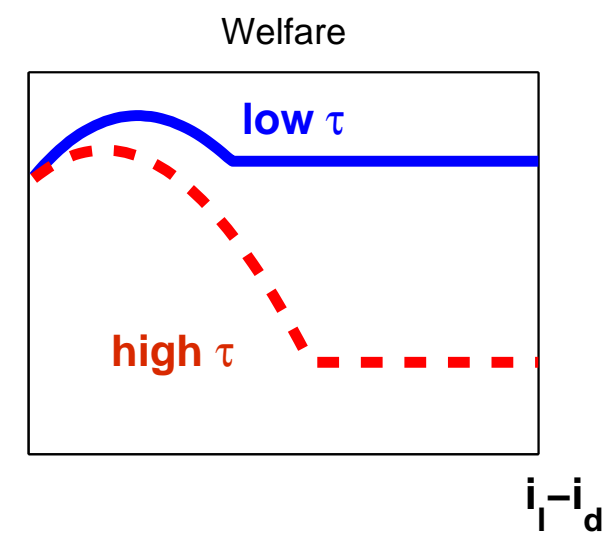
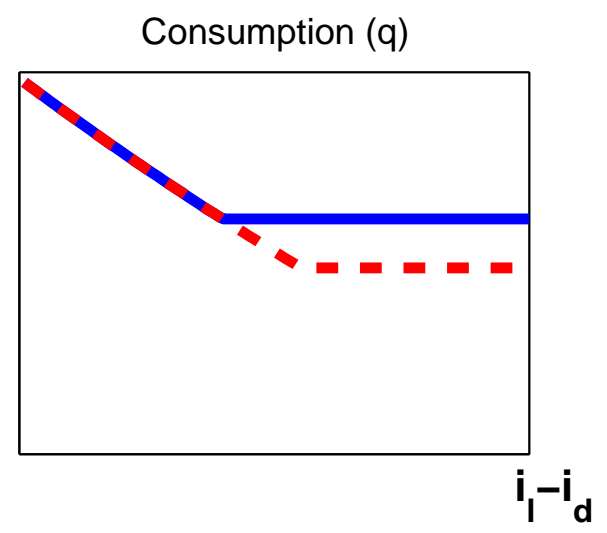
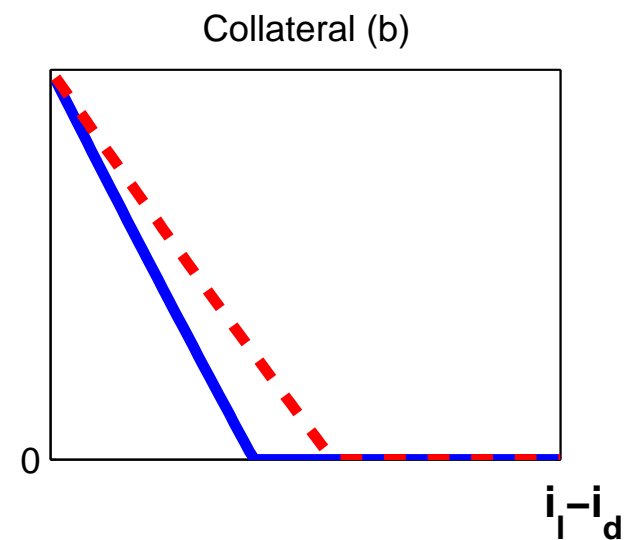
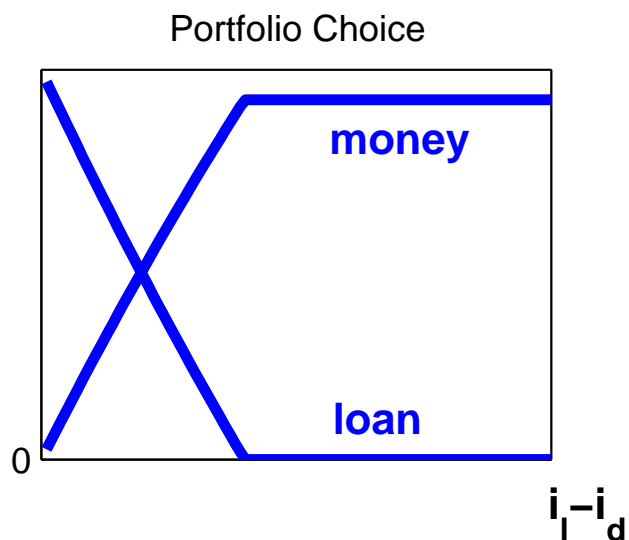
$\Rightarrow b = 0$

$b$  is cheap (high  $R$ )

$\Rightarrow$  low  $i_l$

$\Rightarrow b > 0$

## (2) What is the optimal policy?



### Proposition 2

Optimal Policy:

$b$  is costly (low  $R$ )

$\Rightarrow$  high  $i_l$

$\Rightarrow b = 0$

$b$  is cheap (high  $R$ )

$\Rightarrow$  low  $i_l$

$\Rightarrow b > 0$

$\tau = 0$



## (C) DISCUSSION

Benchmark Case: When money market is inactive ( $\varepsilon = 0$ ):

Optimal Policy:

- Positive Interest Corridor  $i_l - i_d > 0$
- Zero Lump Sum Transfers  $\tau = 0$

QUESTION: How robust are these results?

- ◇ With general cost function
- ◇ With an active money market

## (1) GENERAL COST FUNCTION

For tractability, the paper assumes that the cost of re-balancing portfolio in the settlement market is linear

QUESTION: How robust is the result if we relax the linear cost assumption?

ANSWER:

I numerically computed the case with standard **convex** cost functions and found that:

- ◇ The distribution becomes **non-degenerate**
- ◇ **Positive corridor** is generally still optimal ( $i_l > i_d$ )
- ◇ However, **positive lump sum transfer** can be optimal ( $\tau > 0$ )  
(due to redistributive effect studied in Molico (2006))

## (2) ACTIVE MONEY MARKET ( $\varepsilon > 0$ )

When the money market is active, the paper only derives the equilibrium when “short-selling” constraints are not binding.

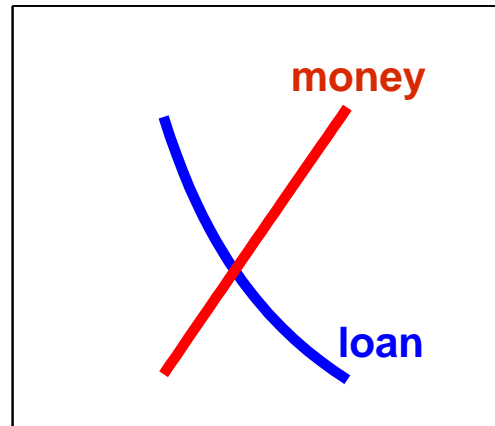
QUESTION: What’s the optimal policy when the money market is active?

ANSWER:

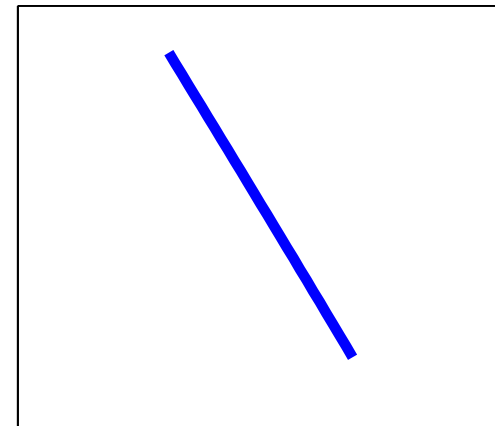
I computed the welfare effects of changing the interest corridor when “short-selling” constraints are not binding.

# OPTIMAL POLICY WITH ACTIVE MONEY MARKET

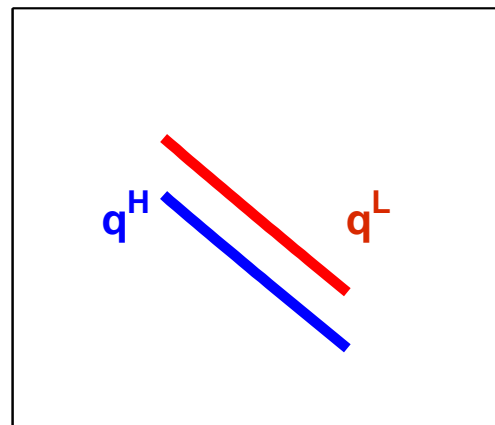
Portfolio Choice

 $i_l - i_d$ 

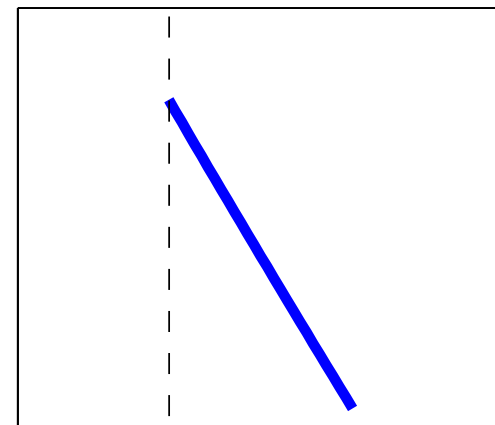
Collateral (b)

 $i_l - i_d$ 

Consumption (q)

 $i_l - i_d$ 

Welfare

 $i_l - i_d$ 

**SHORT-SELLING  
CONSTRAINT**

## (2) ACTIVE MONEY MARKET ( $\varepsilon > 0$ )

When the money market is active, the paper only derives the equilibrium when “short-selling” constraints are not binding.

QUESTION: What’s the optimal policy when the money market is active?

ANSWER:

I computed the welfare effects of changing the interest corridor when “short-selling” constraints are not binding. I found that:

- ◇ Welfare is **decreasing** in the interest corridor.
- ◇ Results suggest that the optimal interest corridor will probably induce **binding “short-selling” constraints.**

## SUMMING UP

- ◇ I learned a lot from this paper.
- ◇ An important first step toward analyzing a channel system in a general equilibrium model.
- ◇ There are some important questions remained unresolved.  
(e.g. optimal policy when money market is active)