

Introduction

- I study a simplified version of Kiyotaki-Moore.
- Entrepreneurs have good projects or bad projects.
- Housing serves as collateral.
- I discuss the properties of a particular equilibrium, with an exploding *bubble* in housing prices.

Equilibrium Dynamics With Stochastic Bubble

- Any positive bubble allows better allocation of capital among entrepreneurs.
 - people with good projects can borrow more b/c collateral is worth more.
- After the bubble bursts, huge redistribution of wealth.
- Output, consumption, wages collapse and then transit slowly to new (lower) SS.
- Capital grows *after* bubble collapses, but is used inefficiently.

Good and Bad Interventions

- Undesirable: give government debt to financial intermediaries.
 - they won't lend the debt to entrepreneurs
 - entrepreneurs have no collateral.
- Desirable: sell government debt at a low price.
- Allocate proceeds of sale to entrepreneurs ("fiscal stimulus").

Model

- Unit measures of entrepreneurs and workers
- Workers simply consume labor income.
- Entrepreneurs have log utility.

- They have technologies $A_t k_t^\alpha n_t^{1-\alpha}$.
- A_t is either 0 or 1 and is iid over time and entrepreneurs.
- Entrepreneurs find out the realization of A_t at date $t - 1$.
- Install capital k_t then, and adjust labor demand at date t .
 - capital depreciates at rate δ .

Housing as Collateral

- Entrepreneurs each have a house.
- A house is an asset with zero consumption services.
- Entrepreneurs trade bonds, capital, and housing.
- Entrepreneurs can borrow up to the value of the house.

Simple, Simple, Simple!

- Entrepreneurs' payoffs are linear in k .
- Face a standard consumption-savings decision at each date.
- With log utility, always consume fraction $(1 - \beta)$ of wealth.

Stochastic Bubble Equilibrium

- One equilibrium works like this ...
- At each date, a coin is flipped, with low probability ε of getting heads.
- If tails, then house price is $p^* > 0$.
- There is a *bubble* in the house price.

- Investors ($A_t = 1$) are always leveraged as much as possible.
- They are able to borrow up to p^* at each date.
- Savers ($A_t = 0$) put almost all of their wealth in housing + bonds.
 - put ε/δ into capital as a hedge.

Key Technical Point: Why do Bubbles Exist in this Model?

- Usually: bubbles can't exist in eq'm b/c they provide an arb. opp.
 - sell house and rent instead
 - NOTE: arbitrage position is an infinitely long one.
- In model: entrepreneurs with good projects are always on their borrowing constraint.
- They hit their borrowing constraint infinitely often along every sample path.
- Can't execute infinitely long arbitrage to exploit the bubble.

Bubble Collapse

- Heads: house price falls to zero and stays there forever.
- Immediate impact is a wealth redistribution.
- Investors' wealths are unchanged, but savers lose almost all their wealth.
- Any intermediary is insolvent - owe savers p^* and have 0 to give them.

- Next period and *forever* after: Output crashes.
 - See Figure 1 in paper.
- Huge need for re-allocation in economy because of iid productivity shocks.
- Without collateral: Capital can no longer be re-allocated efficiently.

Post-Bubble Interventions

- Interventions must cure two problems.
 - entrepreneurs have lost wealth
 - entrepreneurs have lost ability to borrow/lend
- Bad approach: just give government debt to intermediaries.
 - won't work: they won't lend to investors w/o collateral

A Good Plan

- Offer to sell government debt at a low price.
 - that is, raise interest rate (to 0 from $-\delta$).
- Distribute proceeds of sale to entrepreneurs.
- Then roll over debt in future periods.

- I show in paper: government sells exactly p^* worth of debt.
 - savers buy debt and investors don't
 - gov't is an intermediary
- Aggregates immediately return to (and stay at) bubbly steady state.
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Conclusion

- Simple model that allows bubbles to interact with productive activities.
- Provides a way to think about some aspects of current macroeconomic policies and events.
- Missing: Other forms of collateral?