

Comments on Petrin, White, and Reiter  
“The Impact of Plant-level Resource Reallocations and  
Technical Progress on U.S. Macroeconomic Growth”

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# Great research agenda: Where does productivity growth come from?

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## Petrin-White-Reiter

- Decompose Petrin-Levinsohn productivity for manufact. :
  - Weighted plant technology
  - Reallocation



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## Petrin-White-Reiter

## Basu-Fernald (2001, 2002)

- Decompose value-added Solow residual for manufact. :
  - Weighted plant technology
  - Reallocation

- Decompose value-added Solow residual for economy :
  - Weighted industry technology
  - Varying factor utilization
  - Reallocation
  - Average markup/RTS effect

- Extends Basu and Fernald vision to plant-level data !
  - They apply the B-F decomposition, with minor tweaks, e.g.
    - Include average markup in “reallocation”
    - Break out fixed costs explicitly



# Plant-level “technology” includes changes in fixed costs

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- Plant-level estimates of technology (just labor, ignoring plant's relative price):

$$\Delta \ln Q_i = \varepsilon_{iL} \Delta \ln L_i + \Delta \ln \omega_i$$

- Where did it come from?

$$Q_i = G^i(L_i, \tilde{\omega}_i) - F_i$$



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- Where did it come from?

$$Q_i = G^i(L_i, \tilde{\omega}_i) - F_i$$

$$\rightarrow \Delta \ln Q_i = \varepsilon_{iL} \Delta \ln L_i + \left(1 + \frac{F_i}{Q_i}\right) \left(\frac{\partial G^i}{\partial \tilde{\omega}} \frac{\tilde{\omega}_i}{G^i}\right) \Delta \ln \tilde{\omega}_i - \frac{F_i}{Q_i} \Delta \ln F_i$$

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*d ln ω<sub>i</sub>*

Reallocation, defined as gap between “productivity” and technology, includes average markup effect

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$$[\Delta \ln Q_i - c_{iL} \Delta \ln L_i] - \Delta \ln \omega_i = (\varepsilon_{iL} - c_{iL}) \Delta \ln L_i$$

- Typical cost-minimizing FOC implies that  $P_i \frac{\partial Q_i}{\partial L_i} = \mu_i W_i$ , or  $\varepsilon_{iL} = \mu_i c_{iL}$ :
- Labor reallocation =  $(\mu_i - 1) c_{iL} \Delta \ln L_i$

## Puzzle/problem:

Key accounting identity doesn't hold in their data!

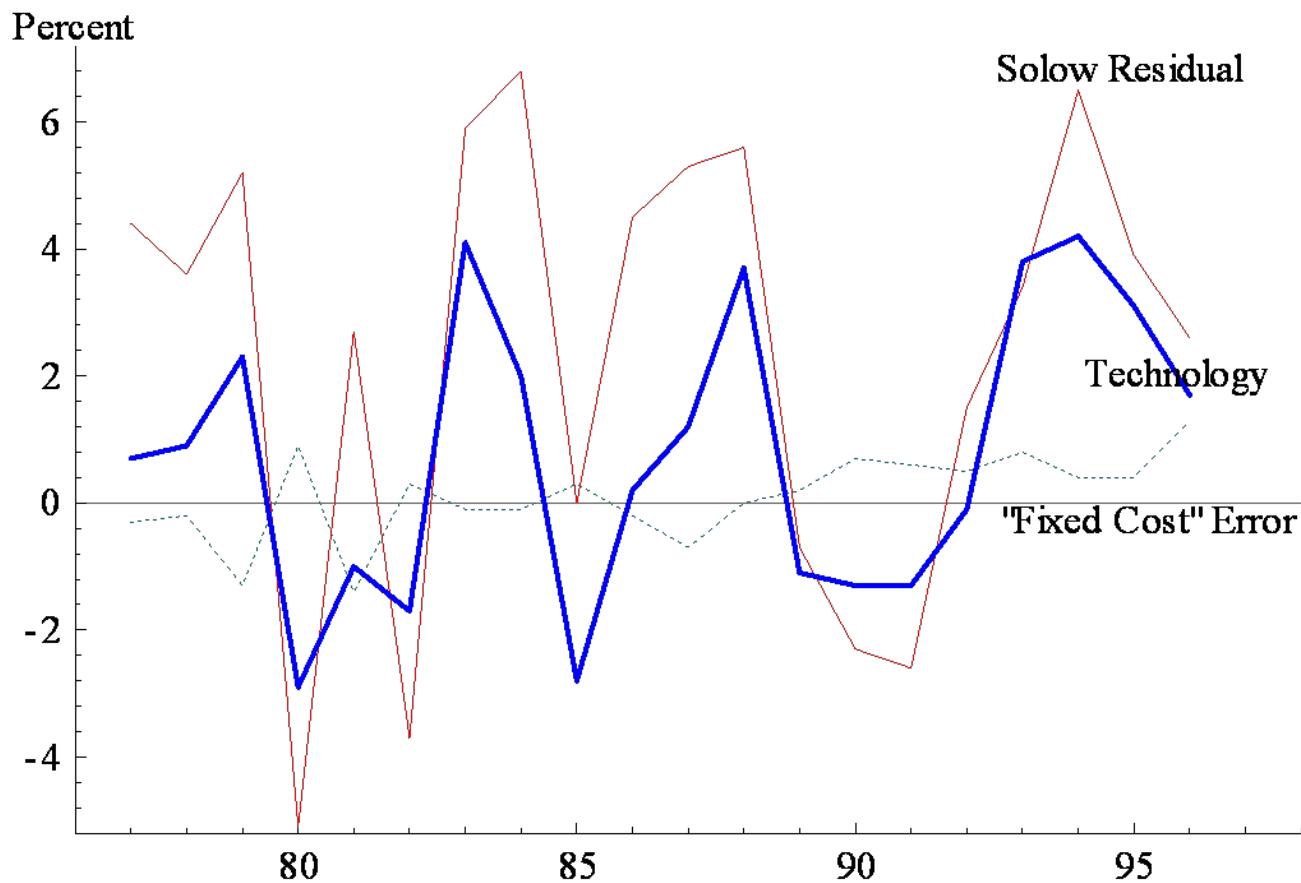
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- Accounting identity is in terms of (unobservables)  $\Delta \ln F_i$  and  $\Delta \ln \tilde{\omega}_i$ , but to be relevant, it needs to be in terms of (measured)  $\Delta \ln \omega_i$ .
  - Want to treat data in identity exactly the same way as in estimation
- Problem: They have an identity and internally consistent data, so shouldn't be a residual!

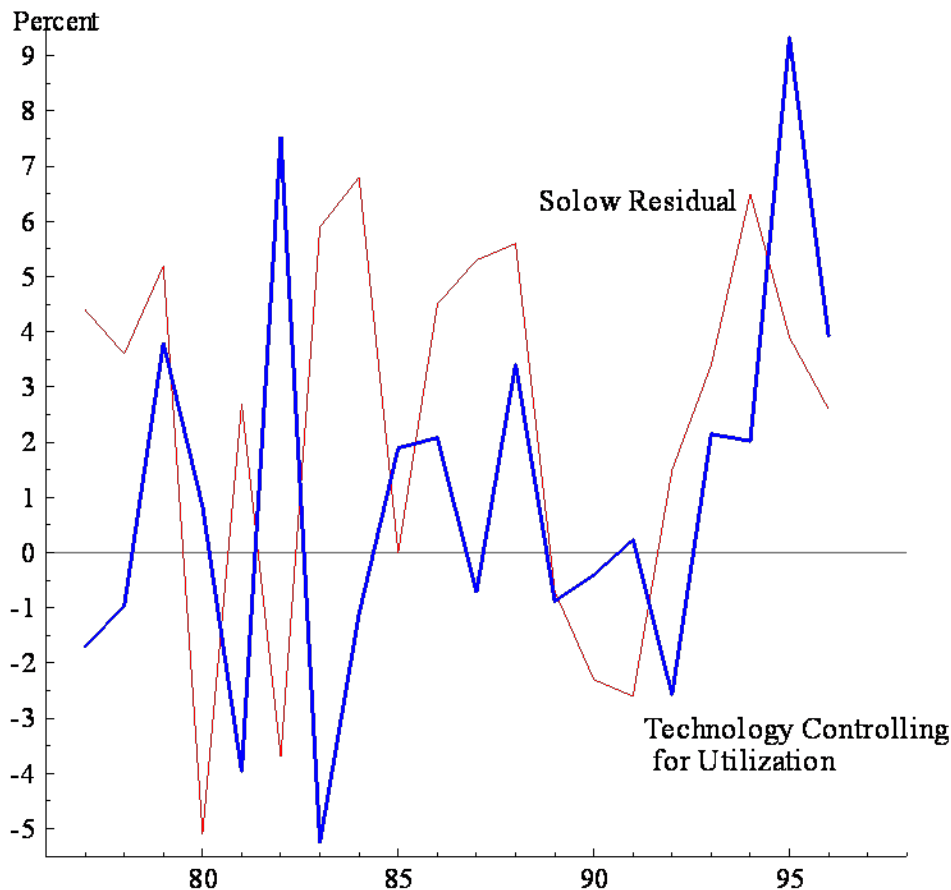


Error seems small and not cyclical, and estimated technology differs noticeably from Solow Residual

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# Controlling for estimated utilization, technology even more different from Solow residual



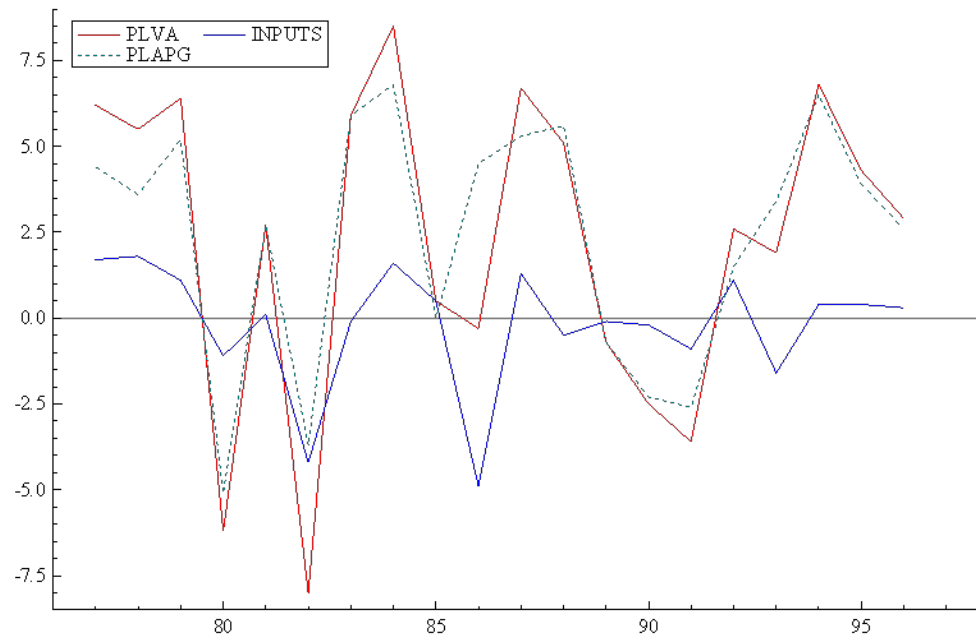
- Basu-Fernald-Kimball (2006) use model-based empirical proxy to control for varying:
  - labor effort
  - Capital's workweek
- Take PWR technology, subtract BFK utilization for manuf.
  - Utilization-adjusted technology is negatively correlated with hours growth

## Wrap-up: Paper takes reasonable approach to identify non-technological component of Solow residuals

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- Technology differs from Solow residual, especially after adding a utilization control
- Relative importance, let alone interpretation, of different reallocation terms isn't established
  - Accounting identity doesn't quite add up
- Question: How important are reallocations *within* two-digit industries, as opposed to *across* industries?





# Extra equations and stuff

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$$\text{FOC: } P_i \frac{\partial Q_i}{\partial K_i} = \mu_i W_i, \text{ or } \varepsilon_{iL} = \mu_i c_{iL}$$

- Their accounting identity is in terms of (unobservables)  $d \ln F_i$  and  $d \ln \tilde{\omega}_i$ , but it needs to be in terms of (measured)  $d \ln \omega_i$ .

$$d \ln VA - c_L d \ln L - c_K d \ln K = \sum_i D_i (\varepsilon_{iL} - c_{iL}) d \ln L_i +$$

# Plant-level “technology” includes changes in fixed costs

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- Plant-level estimates of technology (with just L and K):

$$d \ln Q_i = \varepsilon_{iL} d \ln L_i + \varepsilon_{iK} d \ln K_i + d \ln \omega_i$$

- Where did it come from?

$$Q_i = Q^i(L_i, K_i, \tilde{\omega}_i) - F_i$$

$$\rightarrow d \ln Q_i = \varepsilon_{iL} d \ln L_i + \varepsilon_{iK} d \ln K_i - \frac{F_i}{Q_i} d \ln F_i + \underbrace{\left(1 + \frac{F_i}{Q_i}\right) \left(\frac{\partial Q^i}{\partial \tilde{\omega}} \frac{\tilde{\omega}}{Q^i}\right)}_{d \ln \omega_i} d \ln \tilde{\omega}$$

# Great research agenda:

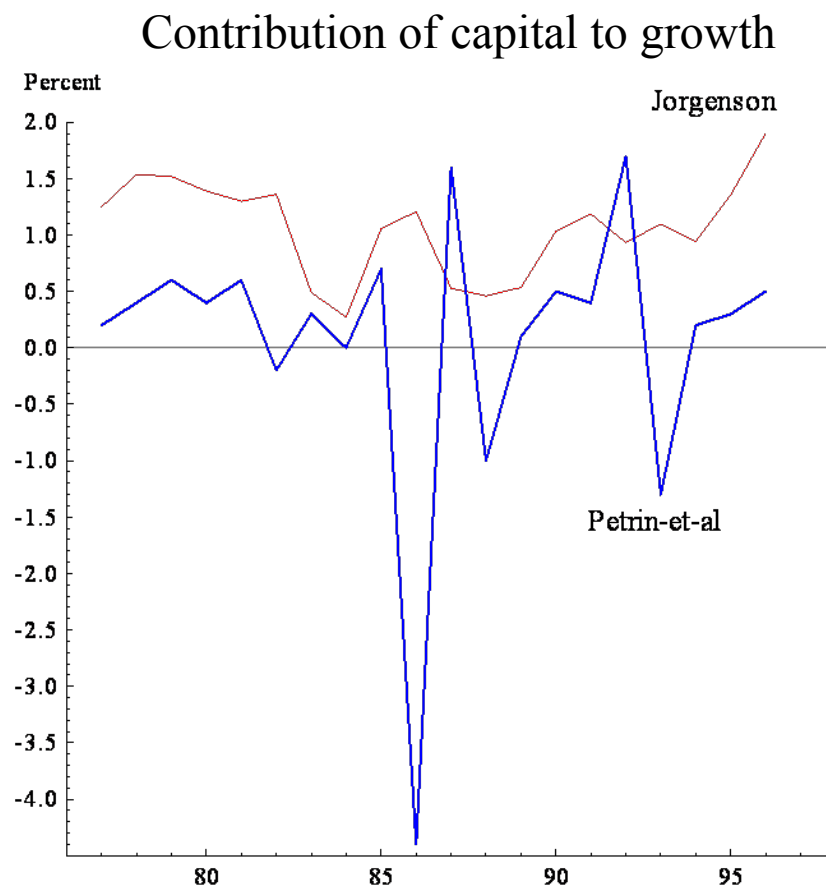
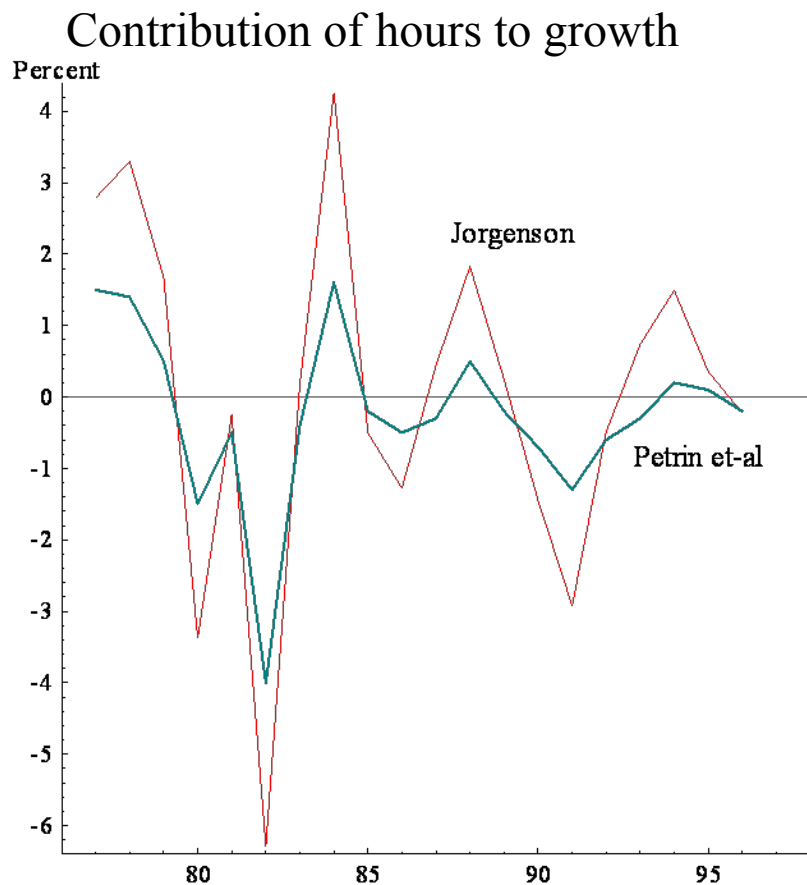
## Where does productivity growth come from?

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- Decompose “Petrin-Levinsohn” productivity for manufacturing into :
  - Weighted plant-level (gross-output) technology
  - Reallocation
- Basu and Fernald (2001, 2002) decomposed value-added Solow residual for entire economy into
  - Weighted industry-level technology
  - Variations in factor utilization
  - Average returns-to-scale/markup effects
  - Reallocation
- Extends Basu and Fernald vision to plant-level data !
  - Petrin-Levinsohn productivity  $\approx$  value-added Solow residual
  - They apply the B-F accounting decomposition, with minor tweaks, e.g.
    - Include average markup in “reallocation”
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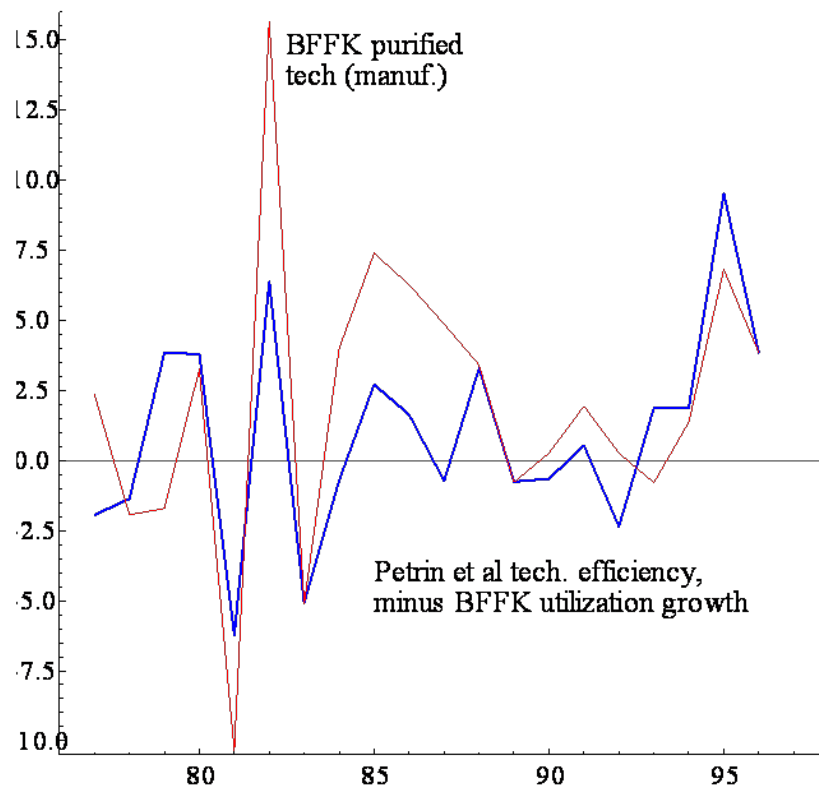
Hours appear excessively smooth, capital excessively volatile...which might affect relative reallocation terms



Note: Series are cost-share-weighted growth in labor and capital inputs, respectively, in Petrin et al compared with Jorgenson's dataset

# Technology corresponds surprisingly well with Basu, Fernald, and Kimball (2006) estimates

Comparing BFK purified “technology” in manufacturing to Petrin et al technical efficiency *less* BFK utilization



- Petrin et al don't control for variable effort or capital's workweek.
- After subtracting BFK estimate of utilization, Petrin *et al*'s technology is close to BFK “purified technology”
  - Correlation is 0.73...
- ...and series is negatively correlated with hours growth