POLICY COOPERATION AMONG BENEVOLENT GOVERNMENTS MAY BE UNDESIRABLE

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ABSTRACT

This paper presents a simple counterexample to the belief that policy cooperation among benevolent governments is desirable. It also explains circumstances under which such counterexamples are possible and relates them to the literature on time inconsistency.

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Since the work of Hamada (1976), investigating the effects of increasing policy cooperation among countries has been a major topic in international economics. A standard conclusion of this work is that increasing policy cooperation among countries is desirable. In a seminal paper, Rogoff (1985) has challenged this view. Using a simple monetary model, Rogoff shows that cooperation among policymakers can lead to a lower level of welfare than non-cooperation does.

Rogoff's result has caused much consternation among those who advocate policy cooperation, and his work has been criticized along several dimensions. For example, some authors, including Canzoneri and Henderson (1988), have noted that a key assumption in Rogoff's model is that the objective function of each country's policymaker does not coincide with the objective function of its residents. Indeed, if in his model policymakers maximize the welfare of their country's residents, the counterexample is overturned and cooperation strictly dominates noncooperation. This feature leads some to interpret Rogoff's result as simply saying that if policymakers form a coalition against the private sector, they may be worse off than if they do not. Others, such as Neck and Dockner (1988), have claimed that Rogoff's result depends on private agents acting strategically. Under this interpretation, Rogoff's result is relevant to, say, economies with a large trade union, but not to economies with a large number of competitive private agents. In a somewhat different vein, Persson (1988) and, especially, Devereux (1986a) have questioned the significance of welfare comparisons across different institutional regimes in a model without a solid foundation for the behavioral relationships.

This paper presents a simple model in which governments are benevolent, but cooperation is still undesirable. The model is a two-country version of Fischer's (1980) optimal tax model. In it, private agents are compe-
titive (in that each agent takes both prices and government policies as uninfluenced by his actions) and each government maximizes the welfare of its country's residents.

In the paper, the two different regimes--cooperative and noncooperative--correspond to alternative institutional arrangements. Neither regime has a technology for committing to a specific set of policy rules at the beginning of time. This feature is modeled by having policymakers move sequentially with private agents. In the noncooperative regime, policies are set separately and sequentially by policymakers to maximize their country's welfare. This institutional arrangement defines an extensive form game. In the cooperative regime, policies are set sequentially by a single decision-making body to maximize world welfare. This institutional arrangement defines another extensive form game. We compare welfare across regimes, using the subgame perfect equilibria of these two games.

The approach used to characterize equilibria of the cooperative and noncooperative regimes may be of some analytical interest. First we show that each regime imposes different dynamic incentive constraints on the set of tax policies. This allows us to characterize the equilibrium allocations of the regimes as solutions to optimal tax problems subject to these constraints. This technique ranks welfare levels in the two regimes without having to resort to a specific numerical example (as in Kehoe 1986).

Finally, note that Van der Ploeg (1987) explored the possibility of undesirable cooperation in a two-country version of Calvo's (1978) inflation tax model using a somewhat different notion of equilibrium than the one used here.

1. THE WORLD ECONOMY

Consider a two-period symmetric world economy consisting of a home country and a foreign country, denoted by \( i = h \) and \( f \). Each country is populated by a
large number of identical consumers and a government. Each country has access to the same linear production function for which the marginal products of labor and capital are denoted by the constants $w$ and $R$. For simplicity, assume [somewhat as Fischer (1980) does] that consumers have consumption-savings-investment decisions in the first period and consumption-labor supply decisions in the second. In the first period, consumers in country $i$ are each endowed with $y$ units of the consumption good out of which they each consume $c^i_1$ and save $s^i$. The consumer then invests some savings, $k^i_h$, in the home country and the rest, $k^i_f$, in the foreign country. In the second period, the individual consumes $c^i_2$ units of the consumption good and $n - n^i$ units of leisure out of a total income of $(1-\theta_h)Rk^i_h + (1-\theta_f)Rk^i_f + (1-\tau_i)wn^i$, where $n$ is the endowment of labor, $\theta_h$ and $\theta_f$ are the tax rates on capital in the home and foreign countries, and $\tau_i$ is the tax rate on labor in country $i$. Assume that savings are completely and costlessly mobile between countries and that labor is immobile.

A consumer in country $i$ chooses $\{c^i_1, s^i, k^i_h, k^i_f, c^i_2, n^i\}$ to solve this:

$$\max[U(c^i_1) + \beta U(c^i_2, n - n^i)]$$

subject to

$$c^i_1 \leq y - s^i$$

$$k^i_h + k^i_f \leq s^i$$

$$c^i_2 \leq (1-\theta_h)Rk^i_h + (1-\theta_f)Rk^i_f + (1-\tau_i)wn^i$$

where $U(c^i_1)$ and $U(c^i_2, n - n^i)$ are both strictly monotone, concave, and smooth and satisfy the usual Inada conditions.

The government of country $i$ sets proportional tax rates on capital income, $\theta_i$, and labor income, $\tau_i$, in order to finance second-period per capita government spending, $g$, which is exogenously given. Let $\pi_i = (\theta_i, \tau_i)$ denote the tax policy of country $i$, and let $\pi = (\pi_h, \pi_f)$ denote the vector of such policies. Each government has monopoly rights to tax all capital and labor.
income earned within its borders; thus each government can earn tax revenue from the investment of foreigners. The budget constraint of government \(i\) is

\[
g \leq \theta_i R(k_i^h + k_i^f) + \tau_i wn^i. \tag{1.2}
\]

Each government \(i\) faces an optimal taxation problem: Choose tax rates \(\pi_i\) to maximize the welfare of a representative consumer of its country, subject to the budget constraint (1.2).

Events in the model are sequential. In the first period, first consumers decide how much to consume and save then governments set tax rates, and finally consumers decide in which country to invest. In the second period, consumers decide how much to consume and work and then governments collect tax revenues. Notice that this timing convention is a simple way to introduce the possibility of capital flight: under it, savings will flee the country that taxes capital income too highly.

The consumer’s problem is conveniently expressed as a two-stage problem. Since the consumer’s budget constraints will bind with equality, they can be substituted out and the home consumer’s problem written as

\[
\max \left[ U(y-s^h) + \beta V^h(s^h, \pi) \right] \tag{1.3}
\]

where

\[
V^h(s^h, \pi) = \max \left\{ \right. \left[ (1-\theta_h)Rk_h^h + (1-\theta_f)R(s-k_h^h) + (1-\tau^h)wn^h, \bar{n}-n^h \right] \left. \right\}
\]

This problem defines the home consumer’s optimal policies for savings, home investment, and labor supply, which are denoted by \(S^h(\pi), K_h^h(s^h, \pi),\) and \(N^h(s^h, \pi)\). Together with the budget constraints, they can be used to obtain the optimal policies for consumption \(c_{1h}(\pi), c_{2h}(s^h, \pi)\) and foreign investment \(k_f^h(s^h, \pi)\). Notice that this notation allows these policies to depend on all four tax parameters, \(\pi = (\theta_h, \tau_h; \theta_f, \tau_f)\). Since labor is immobile, however, these functions do not vary with the foreign tax on labor.
Also, since savings are mobile, consumers will invest all their savings in the
country with the higher after-tax rate of return and thus the lower tax rate
on capital income. Assume that, if the after-tax returns in the countries are
equal, consumers invest all their savings in their own country. The problem
and the optimal policies for a representative consumer in the foreign country
are symmetric.

Consider next the problem of the home government. The objective
function of this government is \( W^h(s^h, \pi) \), where
\[
W^h(s^h, \pi) = U(y-s^h) + \beta U(C^h(s^h, \pi), N^h(s^h, \pi)).
\]

The budget constraint of the home government is
\[
g \leq \theta^h R(K^h(s^h, \pi) + K^f(s^f, \pi)) + \tau^h W^h(s^h, \pi)
\]
where \( K^f(s^f, \pi) \) denotes the foreign consumers' investment in the home country.

Finally, we make two assumptions that will greatly simplify the
computation of equilibrium and the comparison of welfare levels in the two
regimes. First, assume that \( g > R_y \). This condition will guarantee that, in
any equilibrium, labor must always be taxed. Second, assume that financing
government spending solely through a labor tax is always feasible. In Kehoe
(1986), the case in which neither of these conditions hold is analyzed. The
same results hold in that case, however, the computation of equilibrium was
substantially more complicated and required numerical simulations.

2. A NONCOOPERATIVE REGIME

Consider first the regime in which governments set tax rates noncoopera-
tively. At the time the tax rates are set, the savings decisions of the
consumers have already been made. Hence, governments set tax policies as
functions of the level of savings in both countries, \( s^h \) and \( s^f \). Denote these
policies \( \theta^h(s^h, s^f) \) and \( \tau^h(s^h, s^f) \) for the home country and \( \theta^f(s^h, s^f) \) and
\( \tau^f(s^h, s^f) \) for the foreign country. When making its decision, the home govern-
ment takes as given these savings levels, the policy functions of all the consumers, and the policy functions of the foreign government. Thus, the home government chooses tax policy \( \tau_h = (\tau_h, \tau_h) \) as a function of the savings levels, to maximize (1.4) subject to (1.5). The problem of the foreign country is symmetric.

In this noncooperative regime, the **Nash tax policies** are a vector of policy functions \( (\pi_h(s^h, s^f), \pi_f(s^h, s^f)) \) that satisfy each government's budget constraint and

\[
W_h(s^h, \pi_h(s^h, s^f), \pi_f(s^h, s^f)) \geq W_h(s^h, \pi_h(s^h, s^f))
\]

for all \( \pi_h \) that satisfy the home government's budget constraint (and likewise for the foreign government). An equilibrium in this regime is called a **perfect Nash equilibrium** and is defined as a set of allocations \( (c^i, c^i, n^i, s^i, k^i, k^i) \) and tax rates \( \tau_i \) for \( i = h, f \) such that, with \( \pi_h \) and \( \pi_f \) given, the allocations solve the consumer's problem for \( i = h, f \) and the tax rates satisfy \( \pi_i = \pi_i(s^h, s^f) \) for \( i = h, f \).

This equilibrium is characterized in two steps: first, the Nash tax policies for any level of aggregate savings; then, using these, the allocations.

**Proposition 1** (Characterization of the Nash Tax Policies). The Nash tax rates on capital are identically equal to zero. For each \( s^i \), the tax rate on labor \( \tau^i \) is given in the solution to this problem: Choose \( c^i, n^i, \) and \( \tau^i \) to solve

\[
\max U(Rs^i + (1-\tau^i)w, n^i, \bar{n} - n^i)
\]

\[
s.t. \quad U^i_{1}/U^i_{2} = (1-\tau^i)w
\]

\[
g \leq \tau^i w n^i.
\]
Proof. First in any Nash equilibrium the tax rates on capital are identically equal to zero. Clearly, these tax rates cannot be positive. If both were positive, then at least one of the governments could cut its rates, attract all the world's savings, and make itself strictly better off. If only one of the governments set a positive rate, then that government could make itself strictly better off by lowering its rate. Similarly, these tax rates cannot be negative. If either government were subsidizing capital, it could lose less revenue by cutting its subsidy. Since the marginal product of labor is constant, cutting the subsidy would make that country strictly better off. Finally, if one government sets its tax rate on capital identically equal to zero, the other government is indifferent among all possible policies for taxing capital, including the policy in which the tax rate is identically zero. Such a policy is always feasible since, recall, each country can finance its spending solely through a labor tax.

Next for each savings level $s^i$, the Nash labor tax $\tau^i$ is given in the solution to (2.2). Since the foreign labor tax does not enter the home consumer's policy functions, the government's problem immediately reduces to the optimal tax problem in the proposition. \[ \]

Combining the definition of a perfect Nash equilibrium with Proposition 1 and the consumer's problem (1.3) implies immediately that a solution to the following optimal taxation problem is a perfect Nash equilibrium:

\[
\max_{\{s^i, n^i, \tau^i\}} U(y-s^i) + \beta U(Rs^i+(1-\tau^i)wn^i, \bar{n}-n^i) \tag{2.5}
\]

subject to (2.3) and (2.4).

3. A COOPERATIVE REGIME

Consider next the regime in which countries set tax rates cooperatively. Imagine that the two governments set tax rates to maximize the sum of their objective functions subject to their budget constraints. To keep the analysis
simple, concentrate on symmetric equilibria. (For an analysis of the type of complications that arise with asymmetric cooperative equilibria, see Chari and Kehoe 1986.) Of course, when the tax rates are equal, home savings will equal foreign savings, all the home savings will be invested in the home country, and all the foreign savings will be invested in the foreign country. Thus, the problem then resembles that of two closed economies. The superscripts and subscripts can be dropped, and the cooperative problem can be written this way: Taking as given the current state \((s,s)\) and the policy functions of consumers, choose tax schedules \(\theta(s,s)\) and \(\tau(s,s)\) to solve

\[
\max W(s,\pi) \tag{3.1}
\]

s.t. \(g \leq \theta R_s + \tau w N(s,\pi).\)

The policy functions \(\pi(s,s) = (\hat{\theta}(s,s),\hat{\tau}(s,s))\) that solve (3.1) are called the cooperative tax policies. An equilibrium in this regime is a perfect cooperative equilibrium and is defined as a set of allocations and tax rates \(\pi_i\) for both countries that, with \(\pi_h\) and \(\pi_f\) given, the allocations solve the consumer's problem for \(i = h, f\) and the tax rates satisfy \(\pi_i = \hat{\pi_i}(s^h,s^f)\) for \(i = h, f\). We characterize this equilibrium by first solving for the cooperative tax policies. Then we use these to show that the cooperative equilibrium solves an optimal tax problem in which the tax rates on capital are constrained to equal one and the savings levels are constrained to equal zero.

**Proposition 2** (Characterization of the Cooperative Tax Policies). The cooperative tax rates on capital are identically equal to zero. For each \(s\), the cooperative tax rate on labor is given in the solution to this problem: Choose \(n\) and \(\tau\) to solve

\[
\max U((1-\tau)w, n) \tag{3.2}
\]

s.t. \[
U_2/U_1 = (1-\tau)w \tag{3.3}
\]

\(g \leq R_s + \tau w n.\) \(\tag{3.4}\)
Proof. Since savings are already given, they are completely inelastic with respect to the tax on capital. At the time tax rates are set, however, the labor supply decision has yet to be made, so the labor tax distorts the labor supply. To minimize distortions, governments raise as much revenue as they can from the taxation of savings. The assumption that $g > R_y$ implies that even if all the endowment is saved and taxed away, revenues from this tax are less than government spending. Thus, the tax on capital is identically equal to one. Finally, since labor is immobile, home consumers' policies do not depend on the foreign labor tax. Thus, the problem reduces to an optimal tax problem of a closed economy with the capital tax constrained to equal one.

Combining the definition of a perfect cooperative equilibrium with Proposition 2 implies immediately that the solution to this optimal taxation problem is a perfect cooperative equilibrium:

$$\max_{\{n^i, \tau^i\}} U(y) + \beta U((1-\tau)wn^i, \bar{n}-n^i)$$  \hspace{1cm} (3.5)

subject to (3.3) and (3.4).

4. WELFARE COMPARISONS

In Sections 2 and 3, we have seen that the solutions to certain optimal taxation problems are noncooperative and cooperative equilibria. It is easy to show that the cooperative equilibrium is unique and thus problem (3.5) completely characterizes the cooperative equilibrium. Without further restrictions, such as assuming preferences that give rise to linear decision rules, there may be multiple Nash equilibria. Then problem (2.5) characterizes the Nash equilibrium with the highest level of welfare. Since the main purpose of this paper is to provide a counterexample, it is not necessary to characterize all the Nash equilibria, rather it is only necessary to show there is at least one Nash equilibrium which is strictly better than the cooperative equilibrium.
The optimal taxation problems of (2.5) and (3.5) can be used to rank welfare levels of the noncooperative and cooperative equilibria. Notice that the cooperative equilibrium tax problem (3.5) is simply the Nash equilibrium tax problem (2.5) together with the constraint that savings must be zero. Thus, the welfare level in the Nash tax problem is greater than or equal to that in the cooperative problem. It is strictly greater as long as the allocations in the two problems are different, that is, as long as savings are not zero in the Nash equilibrium. A necessary and sufficient condition for the Nash allocation to be strictly preferred is that at the cooperative allocation, \( U'(\hat{c}_1)/U_1(\hat{c}_2, \bar{n}-\hat{n}) < R\delta \) holds, where from the cooperative maximization problem, \( \hat{c}_1 = y \) and \( \hat{c}_2 = \bar{n} - \hat{n} \).

5. DISCUSSION OF ASSUMPTIONS

The model presented in this paper stands as a simple counterexample to the belief that policy cooperation is always beneficial. As such the model has been constructed to be a simple and transparent as possible. In this section we examine some of our simplifying assumptions and point out how they could be generalized.

An assumption that has proved particularly useful is that the production function is linear. It is easy to see that a nearly identical analysis would yield the same results as long as the production function is separable in capital and labor. If instead we assume that this function is non-separable, several parts of the analysis change. In the cooperative regime, the tax rate on capital is still one, but the level of welfare changes. Suppose that the marginal product of labor declines as the capital stock declines. If capital is essential for production, so that this marginal product declines to zero as the capital stock does, no equilibrium will exist. To avoid this, we could assume that some initial capital stock—say \( \bar{K} \)—is untaxable. Then an equilibrium in the cooperative regime would have
k = \bar{k}. Welfare in this regime would decrease as \bar{k} is decreased. The analysis in the noncooperative regime also changes. Since capital increases the marginal product of labor, each government has an incentive to subsidize capital and the Nash tax rates on capital would be negative. In equilibrium, there would be an overabundance of capital. Thus, with a nonseparable production function, the levels of welfare in both regimes change. These levels depend on the shapes of the utility function, the production function, and the initial endowments. By choosing \bar{k} appropriately, we could construct examples in which cooperation is undesirable. We could, however, choose these functions so that cooperation is desirable and thus produce a counterexample to this counterexample.

Another assumption of the model is that all capital is mobile. Instead, we could let there be two types of capital: some stuck in its country and some mobile. Then, in the cooperative regime, governments would tax both types of capital at the same rate. For a high level of government spending, this rate would be one. In the noncooperative regime, the government would tax the immobile capital at rate one and the mobile capital at rate zero. Constructing a counterexample in this case is easy; however, it would just add notation.

Finally, in the model there are two countries and two periods. It is easy to check, either directly or using the general approach of Chari and Kehoe (1986), that as the number of countries is increased, both the noncooperative and cooperative allocations are unchanged. For an analysis of similar environments with an infinite number of time periods, see Kehoe (1987) and Chari, Kehoe, and Prescott (1988).

6. CONCLUSION

The main result in this paper is driven by a time inconsistency problem that arises even with benevolent governments. One interpretation of this type of
problem is the following. Given a technology for commitment and a closed economy, the relevant tax problem of the government is the static Ramsey problem. Without such a technology, however, the relevant tax problem is this static problem together with dynamic incentive compatibility constraints. For the model these constraints require that the tax on capital be equal to one. In a two-country world, the cooperative regime has these same constraints. In a noncooperative regime, in contrast, the competition among governments produces a different set of dynamic incentive constraints—namely, that the tax on capital always be zero—and the resulting level of welfare may be higher. It should be clear that what drives the result is not a conflict between the governments and their own citizens, but rather that the different institutional arrangements produce different dynamic incentive constraints. Loosely, the intuition for the result is that, in a dynamic economy where government commitment is not feasible, competition among governments may act like partial commitment and hence may be preferred to cooperation.

Consider a situation in which governments have no access to a commitment technology, are currently in a noncooperative regime, and are contemplating setting up a new institution through which governments cooperate. This paper shows that the value of such an institution may well be negative. Of course, if it is feasible to set up an institution through which governments can simultaneously guarantee both commitment and cooperation then they should do so and everyone would be better off.

In the paper, we have compared welfare under alternative arrangements. In one, policymaking is decentralized among competing policymakers; in the other, it is centralized in a single decisionmaking body. Extending this type of analysis to other settings would be interesting. For example, consider a country composed of many states. One could ask, Is it better to decentralize policymaking by letting each state choose its own tax and spend-
ing policies or to centralize this policymaking in one decisionmaking body? Is it better to establish separate entities governing monetary and fiscal policies or to have one entity that decides both?

Finally, although the model in this paper is constructed mainly to produce a counterexample, it is somewhat interesting in its own right. The model suggests that the possibility of capital flight in a strategic setting may make the analysis of taxation in an open economy drastically different from that in a closed economy. Another approach would be to analyze the alternative tax equilibria in a model with a more detailed tax structure, perhaps in a calibrated, multicountry, general equilibrium model.
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