

# Connecting Asset and Labor Markets in a Heterogeneous Agent Model

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## Disclaimer

- The views expressed in this talk are my own.
- They may not be shared by others in the Federal Reserve System ...
- Especially my colleagues on the Federal Open Market Committee.

## **Acknowledgements**

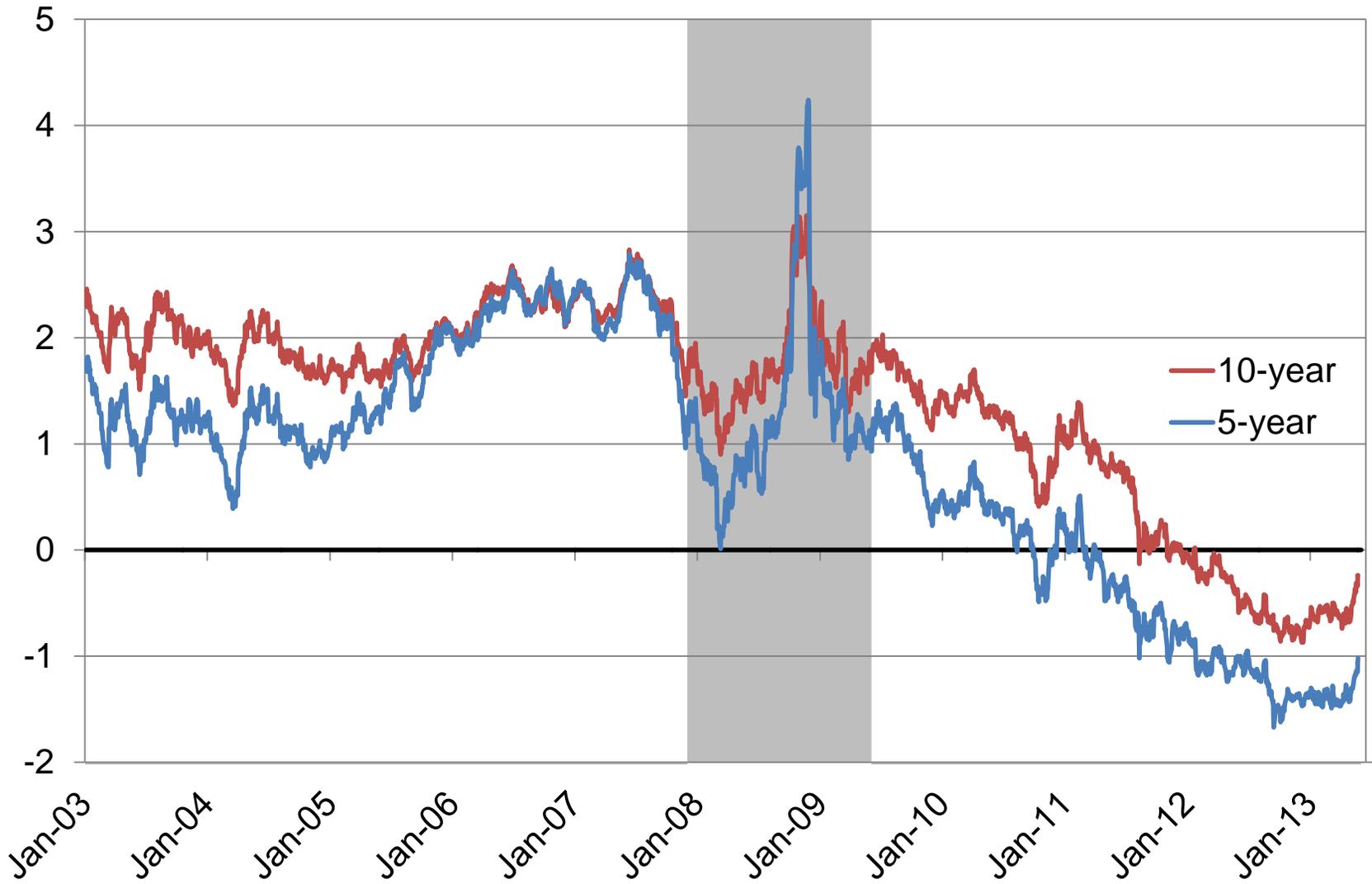
I thank participants in a FRB-Minneapolis bag lunch for comments.

## Changes in Asset Markets

- There have been changes in asset markets since 2007.
  - Borrowing constraints have tightened.
  - Increase in perceived macroeconomic risk.
  - Decline in supply of "risk-free" assets.
- Combined effect: increase in net asset demand.
- These changes seem likely to reverse only slowly.

# Treasury Real Yield Curve Rates

Percent



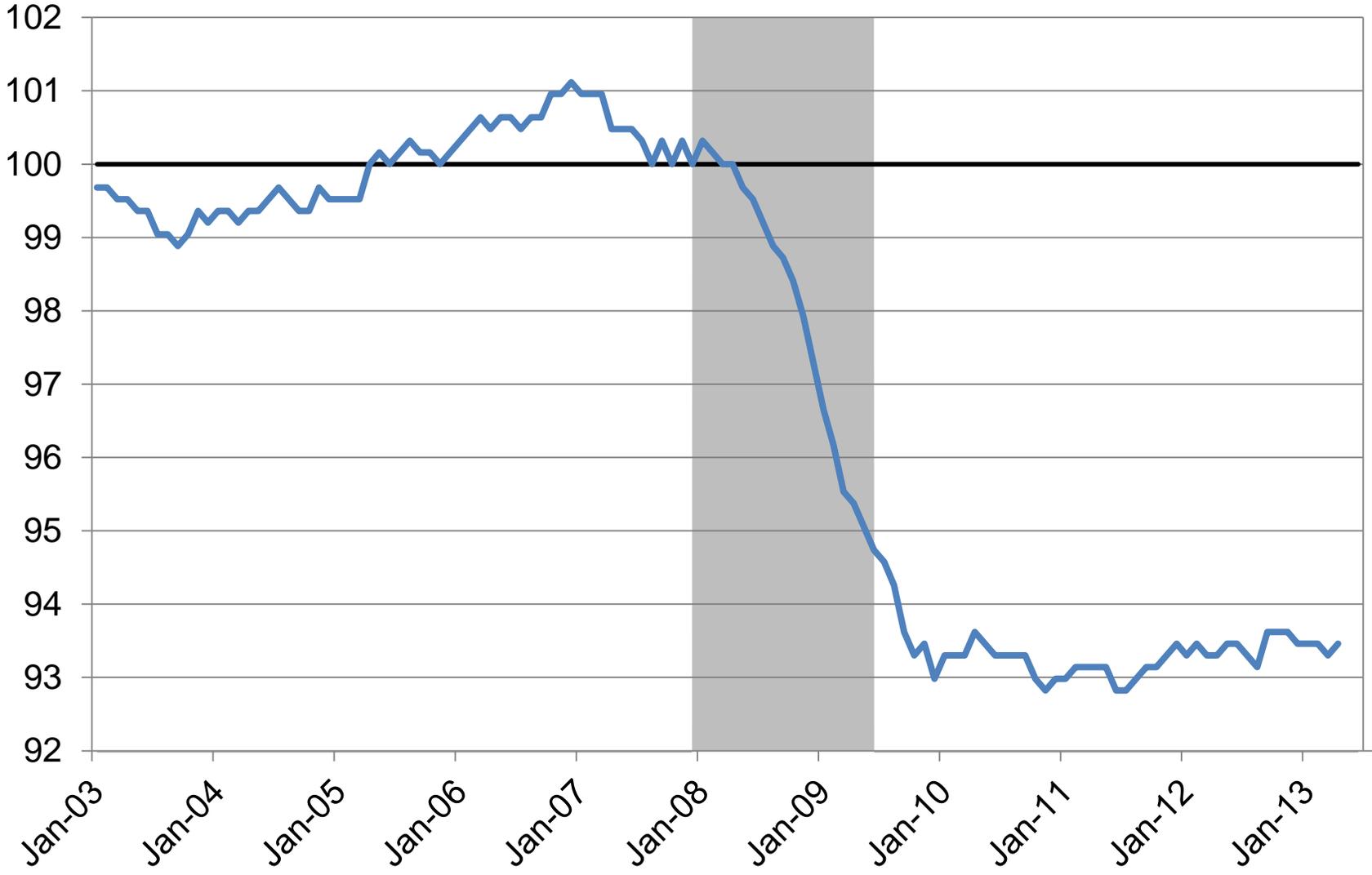
Source: U.S. Department of the Treasury

## Changes in Employment

- Employment/population in US fell sharply from late 2007 to late 2009.
- This change has been highly persistent:
- Employment/population has risen little since late 2009.

# Employment-Population Ratio

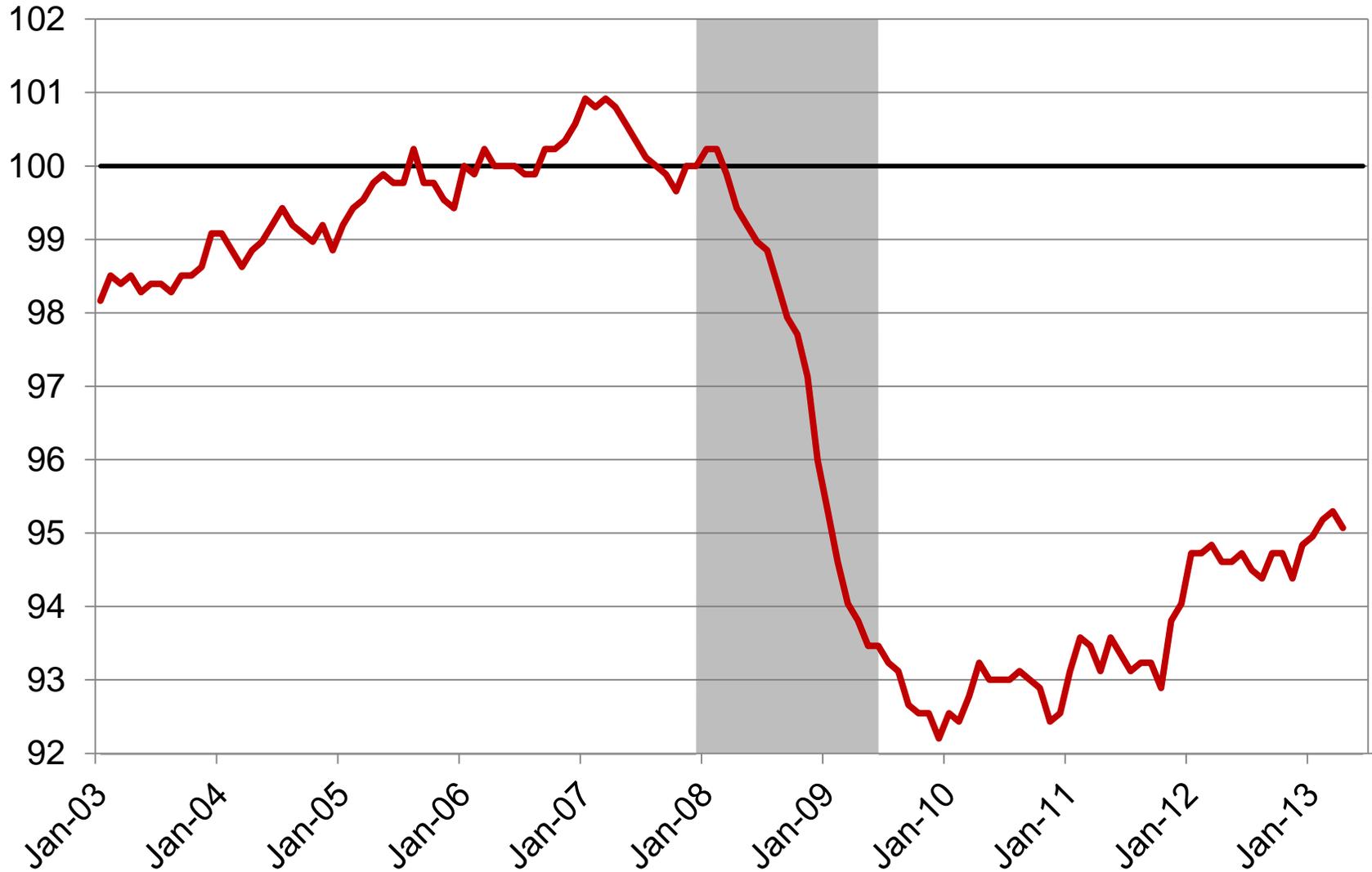
Index: December 2007 = 100



Source: Bureau of Labor Statistics

# Employment-Population Ratio, Men 25-54

Index: December 2007 = 100



Source: Bureau of Labor Statistics

## Connecting the Two Changes: The Model

- In this talk, I link these two persistent changes.
- I use a *heterogeneous agent model* with:
  - **inelastic labor supply** (recent micro-evidence on extensive margin)
  - **incomplete insurance markets** (Bewley-Huggett)
  - **flexible** or **rigid** nominal wage growth

## Connecting the Two Changes: The Shock

- I posit a permanent exogenous increase in net asset demand.
  - Many possible sources of this shock - I use tighter borrowing constraints
- The impact of this shock depends on the flexibility of wages.

## **Connecting the Two Changes: The Results**

**If wages are flexible:**

The shock has no impact on employment.

**If nominal wage growth is fixed (can't rise):**

The shock causes employment to fall unless monetary policy is eased enough.

## Intuition for Flexible Case

- Key equilibrating mechanism:
  - Excess labor supply pushes up nominal wage growth.
- In turn, anticipated inflation rises.
- People buy more goods today and firms demand more workers ...
- Until labor markets clear.

## Intuition for Rigid Case

- Suppose nominal wage growth can't rise.
- Then anticipated inflation can't rise.
- If the nominal interest rate is not lowered enough, then ...
- The real interest rate doesn't fall enough.
- Product demand remains too low, and employment is too low.

## Outline

1. Model
2. Equilibrium
3. Comparative Statics
4. Conclusions

MODEL

## Preferences: Consumption

- Unit measure of agents.
- Each agent maximizes expected value of:

$$\sum_{t=1}^{\infty} \beta^{t-1} u(c_t), 0 < \beta < 1, u', -u'' > 0$$

where  $c_t$  is consumption in period  $t$ .

## Preferences: Labor

- At each date, each agent wants to work ( $\bar{a} = 1$ ) or not ( $\bar{a} = 0$ ).
- The binary state  $\bar{a}_t$  is a Markov chain with transition matrix  $\Phi$ .
- The autocorrelation of  $\bar{a}$  is non-negative.
- No aggregate shocks (evolution is iid across agents).

## Involuntary Non-Employment

- Conditional on  $\bar{a} = 1$ , an agent's labor  $\bar{n}$  is equal to:
  - 1 with probability  $(1 - \mu)$ .
  - $\varepsilon$  ( $\varepsilon$  small but positive) with probability  $\mu$ .
- Conditional on  $\bar{a} = 0$ , an agent's labor  $\bar{n} = 0$ .
- The variable  $\mu$  is endogenous, while  $\Phi$  is exogenous.
- I refer to  $\mu$  as *labor market slack*.

## Technology

- There are a large number of competitive firms.
- Firms produce  $zN$  units of consumption with  $N$  units of labor.

## Trading

- At each date, agents trade a one-period risk-free nominal bond.
- Bonds are available in zero net supply.
- Nominal interest rate is set by monetary policy.
- Agents face a real borrowing limit  $b^*$ .

## Budget Set

$$P_t c_t + B_{t+1}/(1 + R) \leq W_t \bar{n}_t + B_t$$

$$B_{t+1} \geq -P_{t+1} b^*$$

EQUILIBRIUM

## Budget Equivalence

- Agents have budget sets defined by:

$$P_t c_t + B_{t+1}/(1 + R) \leq W_t \bar{n}_t + B_t$$

$$B_{t+1} \geq -b^* P_{t+1}$$

- Define (and assume time invariance of):

$$r \equiv \frac{(R - \pi)}{1 + \pi}$$

$$\pi \equiv \frac{P_{t+1} - P_t}{P_t}$$

$$w \equiv \frac{W_t}{P_t}$$

- Divide original budget set through by  $P_t$  and define  $b_t = B_t/P_t$ .

- We get equivalent (Bewley-Huggett) budget sets:

$$c_t + \frac{b_{t+1}}{1+r} \leq w\bar{n}_t + b_t$$

$$b_{t+1} \geq -b^*$$

## Bewley-Huggett Demand Functions

- Suppose agent has budget set:

$$c_t + b_{t+1}/(1 + r) \leq w\bar{n}_t + b_t$$

$$b_{t+1} \geq -b^*$$

- Labor  $\bar{n}_t$  follows the Markov chain determined by:
  - $\Phi$  (exogenous transition of willingness to work)
  - $\mu$  (endogenous labor market slack)

- Let  $\bar{b}^d(r; b^*, \mu, w)$  be (long-run) average bondholdings.
- **Result:**  $\bar{b}^d$  is weakly decreasing in the borrowing limit  $b^*$ .
- **Result:**  $\bar{b}^d$  is increasing in the real interest rate  $r$ .
- **Assumption:**  $\bar{b}^d$  is decreasing in labor market slack  $\mu$ .

## Stationary Equilibrium

- Wage inflation  $\pi_W$ , price inflation  $\pi$ , and slack  $\mu$  satisfy:

$$\pi_W = \pi \quad \text{(firm optimality)}$$

$$\bar{b}^d\left(\frac{R - \pi}{1 + \pi}; b^*, \mu, z\right) = 0 \quad \text{(asset mkt clears)}$$

- Need a third equilibrium condition somewhere!

## Flexible Wage Equilibrium

- Flex-wage equilibrium conditions:

$$\pi_W = \pi \quad \text{(firm optimality)}$$

$$\bar{b}^d\left(\frac{R - \pi}{1 + \pi}; b^*, \mu, z\right) = 0 \quad \text{(asset mkt clears)}$$

$$\mu = 0 \quad \text{(no slack)}$$

- Nominal wage growth adjusts so that there is no labor market slack.

## Equilibrating Mechanism

- Suppose the labor market is out of equilibrium ( $\mu > 0$ ).
- Households bid down current wages (relative to future wages).
- Counterintuitive (?): labor market slack pushes **up** wage growth.

- Product competition: higher wage growth means more inflation.
- People demand more consumption and firms demand more labor.
- Process continues until  $\mu = 0$ .

## Rigid Wage Equilibrium

- Rigid wage eq'm: wage inflation is exogenous ( $\bar{\pi}_W$ ).
- Rigid wage equilibrium conditions:

$$\pi_W = \pi \quad \text{(firm optimality)}$$

$$\bar{b}^d\left(\frac{R - \pi}{1 + \pi}; b^*, \mu, z\right) = 0 \quad \text{(asset mkt clears)}$$

$$\pi_W = \bar{\pi}_W \quad \text{(rigid wage growth)}$$

- The real interest rate is exogenous.
- Asset market clears via changes in labor market slack.

## Equilibrating Mechanism

- Suppose the asset market is out of equilibrium:

$$\bar{b}^d\left(\frac{R - \bar{\pi}_W}{1 + \bar{\pi}_W}; \mu, b^*, z\right) > 0.$$

- Too much asset demand implies that there's too little product demand.
- Given that low product demand, firms scale back labor demand ( $\mu$  rises).
- With less labor income, asset demand falls until market clears.

# COMPARATIVE STATICS

## Experiments

- How does eq'm output depend on borrowing constraint  $b^*$ ?
- How does eq'm output depend on monetary policy  $R$ ?
- The answer depends on eq'm notion (flex or rigid).

## Flexible Wage Equilibrium

- In equilibrium, for any  $R$  or  $b^*$ , slack  $\mu$  equals 0.
- The borrowing limit and monetary policy don't affect aggregate quantities.

- But they do affect equilibrium outcomes.
- Suppose the borrowing constraint is tighter ( $b^{**} < b^*$ ) ...
- Or monetary policy is tighter ( $R^{**} > R^*$ ).
- Both of these changes push up on asset demand.

- To clear asset market, the real interest rate must fall.
- That's accomplished via an **increase** in nominal wage growth:

$$\pi^{**} = \pi_W^{**} > \pi_W^* = \pi^*$$

## Rigid Wage Equilibrium

- Wages grow at exogenous rate  $\bar{\pi}_W$ .
- Competition among firms implies that inflation  $\pi = \bar{\pi}_W$ .
- The real interest rate adjusts through changes in monetary policy ( $R$ ).

- Suppose the borrowing constraint tightens ( $b^{**} < b^*$ ) ...
- OR monetary policy tightens ( $R^{**} > R^*$ ) ...
- These changes push up on asset demand.

- The real interest rate can't adjust because  $R$  and  $\pi_W$  are fixed.
- To clear asset market, labor market slack must rise:

$$\mu^{**} > \mu^*$$

- The rise in slack pushes down on income and so on asset demand.

## Conclusions

- Suppose borrowing limit ( $b^*$ ) shrinks.
- This fall in the borrowing limit increases net asset demand.
- How does this increase in asset demand affect labor markets?

- Impact on labor markets depends on wage adjustment.
- Flexible wages: no effect on output or employment.
- Rigid wages: output and employment fall.
  - This decline can be offset with easier monetary policy.

# CONCLUSIONS

## Changes Since 2007

- A number of changes in asset markets since 2007.
- Asset demand has risen:
  - increased uncertainty
  - lower potential growth estimates
  - tighter borrowing constraints

- Outside supply of risk-free assets has fallen.
  - Sovereign debt is riskier.
  - US land values are lower - and land is riskier.
  - Partial offset: increase in sovereign debt.
  
- Overall: Net asset demand has risen.

## Implications of a Heterogeneous Agent Model

- I used a standard incomplete financial markets model.
- After an increase in net asset demand, asset markets clear via:
  - a fall in the real interest rate
  - OR a fall in economic activity

- Suppose nominal wage growth is fixed, so it can't rise.
- Then the real interest rate depends only on  $R$  (monetary policy).
- If  $R$  is kept too high (ZLB?), then the real interest rate won't fall enough.
- And the asset demand shock results in a fall in economic activity.

## Modern Models, Old Implications

- The analysis is based on a standard workhorse "modern macro" model.
- It delivers neoclassical conclusions if wages are flexible.
- It delivers Keynesian conclusions if ...
- Nominal wage growth fails to rise enough to eliminate excess labor supply.

## Future Research

- The question is:

**How do nominal wages respond to excess labor supply?**

- We need a lot more work on this question.
- Useful approaches: micro-evidence and surveys.